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THE GREAT RECESSION: A SELF-FULFILLING GLOBAL PANIC

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The Great Recession: A Self-Fulfilling Global Panic*

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Abstract

While the 2008-2009 financial crisis originated in the United States, we witnessed steep declines in output, consumption and investment of similar magnitudes around the globe. This raises two questions. First, given the observed strong home bias in goods and financial markets, what can account for the remarkable global business cycle synchronicity during this period? Second, what can explain the difference relative to previous recessions, where we witnessed far weaker co-movement? To address these questions, we develop a two-country model that allows for self-fulfilling business cycle panics. We show that a business cycle panic will necessarily be synchronized across countries as long as there is a minimum level of economic integration. Moreover, we show that several factors generated particular vulnerability to such a global panic in 2008: tight credit, the zero lower bound, unresponsive fiscal policy and increased economic integration.

1.   Introduction

The 2008-2009 Great Recession clearly had its origins in the United States, where an historic drop in house prices had a deep impact on financial institutions and markets. It is remarkable then, as illustrated in Figure 1, that the steep decline in output, consumption and investment during the second half of 2008 and beginning of 2009 was about the same in the rest of the world as in the United States.[1] This is surprising both in the context of existing theory and historical experience. Transmission channels in existing models depend critically on trade and financial linkages and on the type of shocks. A recent literature has shown that it is possible to have one-to-one transmission of shocks if goods and financial markets are perfectly integrated and there are credit rather than technology shocks.[2] But in reality goods and financial markets are far from perfectly integrated and there is significant home bias in both goods and asset trade. As illustrated in van Wincoop (2013), a model with credit shocks that captures the observed financial home bias will have partial transmission at best. Consistent with this, Rose and Spiegel (2010) and Kamin and Pounder (2012) find that there is little relation between financial linkages that countries have with the U.S. and the decline in their GDP growth and asset prices during 2008-2009.[3]

The close co-movement of business cycles illustrated in Figure 1 is also unusual from an historical perspective. Figure 2 shows that during the Great Depression the decline in output in the rest of the world was much smaller then in the United States. Perri and Quadrini (2012) show that business cycle co-movement during the 2008-2009 recession stands out significantly relative to previous recessions since 1965. Hirata, Kose and Otrok (2013) find that over the past 25 years the global component of business cycles has actually declined relative to local components (region and country-specific). This then leads to two questions that we aim to address in this paper. First, given the limited extent of goods and financial integration, how can we explain that the sharp decline in business cycles was similar in the rest of the world as in the United States during the Great Recession? Second, what can explain the difference relative to previous recessions?

To answer these questions we develop a two-country, two-period New Keynesian model that explains the recession as resulting from a self-fulfilling shock to expectations as opposed to an exogenous shock to fundamentals. The self-fulfilling beliefs are a result of several inter-linkages between the present (period 1) and the future (period 2). The future affects the present as beliefs of lower and riskier second-period income lead to higher first period saving. As consumption falls, output and firm

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[1]   Even outside of Europe, which had by far the largest foreign exposure to U.S. asset backed securities, the business cycle decline was of similar magnitude.

[2]   Examples are Devereux and Sutherland (2011), Kollmann, Enders and Muller (2011) and Perri and Quadrini (2012). It is well known that with technology shocks output tends to be negatively correlated across countries even in models with perfect goods and financial market integration.

[3]   Kalemli-Ozcan et al. (2013) find that financial integration has a negative effect on business cycle synchronization outside of crisis times and a zero effect during crisis times. They also find that the bulk of the increase in synchronization during the 2008-2009 crisis is associated with an undetermined common shock.

profits decline.[4] But the present also affects the future as lower profits lead to an expectation of lower future economic activity and greater sensitivity of firms to future shocks. This lowers expected future output and increases uncertainty about future output. Figure 3, which is based on survey data, shows that there was indeed a large drop in expected GDP growth and an increase in its perceived variance. Moreover, these changes in beliefs were of similar magnitude in the rest of the world as in the United States.[5]

A key result of the model is that a business cycle panic is necessarily synchronized across the two countries as long as they have some minimum level of trade and financial integration. The drop in output, consumption and investment will then be of equal magnitude in the two countries. When trade and financial linkages are very weak, it is possible to have a business cycle panic that is limited to just one country. This is no longer possible when there is sufficient economic integration. Intuitively, either the country that panics drags the other country into a panic or the country that does not panic pulls the other country out of the panic. Their interconnectedness makes it impossible for one country to have self-fulfilling negative beliefs about the future while the other country has favorable beliefs about the future. Limited interconnectedness then implies that their fate will be common. A panic, if it happens, will necessarily be global. The threshold level of economic integration does not need to be high. It is therefore possible to still have significant home bias in trade and asset holdings as seen in the data.

The model also provides an explanation for the difference relative to previous recessions. Limited co-movement of business cycles in open economy models is usually the result of partial transmission (through trade and financial linkages) of exogenous country-specific shocks. That may well be a good description for most business cycles. However, in our model the co-movement is not a result of transmission but rather of a coordinated panic. A combination of distinct factors, all featured in the model, made the 2008 period particularly vulnerable to such a global self-fulfilling panic. First, credit was tight. We show that when credit conditions are easier, self-fulfilling panics are not feasible in equilibrium. Tight credit makes firms more susceptible to default when hit by a drop in demand that lowers profits. This is a critical element in our model of self-fulfilling beliefs. Second, interest rates were low, close to the zero-lower bound. This reduces the potential stabilizing role of monetary policy since it is easier to fall in a liquidity trap. Third, there were constraints on countercyclical fiscal policy, especially due to historically high debt levels. Fourth, the world has experienced a significant increase in both trade and financial integration over the past two decades. The model then implies that panics are more likely to be common across countries.

The crisis in U.S. financial markets plays a role in our theory of a global recession, but only as a trigger event for the self-fulfilling shift in beliefs. This stands in contrast to models in which the linkage

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[4]   This relates to the classic Paradox of Thrift, where higher saving implies lower demand, which reduces output and may actually end up lowering saving. We will discuss the Paradox of Thrift in the context of our model in Section 5. For recent contributions, see Eggertsson and Krugman (2012), Eggertsson (2010) and Christiano (2004).

[5]   The data comes from Consensus Economics, who survey about 250 "prominent financial and economic" forecasters. Each January, forecasters are asked to give probabilities for GDP growth rate intervals for the current year. We compute the average and the variance for each country, as explained in more detail in Appendix A. For the non-US data line, we use the average across the 17 other countries in the sample.

between financial markets and the real economy operates through a credit shock or a decline in wealth. While credit was tight, it is hard to argue that there was a large global credit shock. Figure 4 shows BIS data on total credit to the private sector for the U.S. and non-U.S. G-7 countries. Two points stand out. First, the experience of the non-U.S. G7 was quite different from that in the U.S., with a continued increase in private credit during and after the crisis. Second, while in the U.S. there was a decline in private credit since 2008, this decline was gradual and continued through 2012. The main source of credit decline was the gradual deleveraging of U.S. households, which was not concentrated during the period of the sharp output decline in late 2008 and early 2009.[6] It is also hard to argue that a decline in wealth was responsible for the global recession. With the exception of some smaller European countries (Ireland and Spain) the sharp decline in housing wealth was a U.S. phenomenon rather than a global phenomenon.[7]

The paper is related to some other recent work on self-fulfilling business cycle panics.[8] The most important difference is that these are closed economy models and therefore do not address the co-movement question. Farmer (2012a, b) analyzes models where self-fulfilling beliefs are associated with wealth. A belief of a lower value of financial wealth leads to lower consumption, which leads to lower firm profits, which justifies the drop in wealth. But as just pointed out, the decline in wealth was much smaller in the rest of the world than in the United States.

Heathcote and Perri (2012) also have a model where the decline in wealth is critical to self-fulfilling beliefs, although through a different mechanism. In their model lower housing wealth makes it possible to have self-fulfilling beliefs of higher unemployment. If households find it less likely that they have a job tomorrow, and it is hard to borrow when their housing collateral is low, they will reduce consumption. This reduces output, which indeed leads to more unemployment. Both this paper and the Farmer papers rely on labor market rigidities rather than nominal rigidities to generate a link from demand to production.

Benhabib, Wang, and Wen (2012) develop a model where business cycles are affected by market sentiments when production decisions need to be made in advance of knowing demand and agents receive imperfect information about aggregate demand. It has in common with the Farmer papers that

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[6]   Chari, Christiano and Kehoe (2008) document that bank credit actually increased in the U.S. during the second half of 2008 (both consumer and industrial bank credit). Adrian, Colla and Shin (2011) find that a decline in bank credit to firms in 2009 was replaced by an equal increase in bond financing. Also consistent with the absence of a large credit shock, Kahle and Stulz (2013) use firm level data to show that there was no relationship between the drop in investment by firms and their bank dependence. Helbling, Huidrom, Kose and Otrok (2011) estimate a global VAR to find that a global credit shock accounts for only 10% of the global drop in GDP in 2008-2009.

[7]   While stock markets declined significantly everywhere, they tend to be less important in most countries than in the United States.

[8]   See Schmitt-Grohé (1997) for a review of earlier models.

the business cycle then depends on a market sentiment variable that can take on a continuum of values, as opposed to models such as ours where there is either a panic or not.[9]

Finally, Perri and Quadrini (2012) introduce a mechanism leading to self-fulfilling credit shocks. If the resale value of firms is expected to be low, credit will be tight. But tight credit makes it difficult for constrained firms to purchase assets from defaulting firms, which indeed makes the resale value low. While they have a two-country model with perfect business cycle co-movement, this is a result of perfect financial and goods market integration.[10]

To present the basic mechanism, we analyze a benchmark model without investment, financial asset trade or uncertainty. In that context, it is possible to derive theoretically the conditions under which global panics occur. Our main result, stated in Proposition 2, is that partial integration is sufficient to guarantee that business cycles are perfectly synchronized during a panic. We show numerically that the extent of integration required is relatively small. A panic limited to one country is not possible with sufficient integration. When we extend the model to include investment, financial asset trade and uncertainty, the results are similar but can only be derived numerically.

The remainder of the paper is organized as follows. Section 2 describes the benchmark model. Section 3 analyzes the equilibria and determines when business cycle panics are global. Section 4 shows that countries are more vulnerable to global panics with tight credit, low interest rates or rigid fiscal policies. Section 5 considers various extensions and Section 6 concludes.

2.   The Model

In this section we describe the benchmark model. There are two countries, Home and Foreign, and two periods, 1 and 2. The basic two-period New Keynesian structure is similar to closed economy models found in the literature, starting with Krugman (1998).[11] Prices are pre-set, while wages are flexible. There is partial integration of goods markets through trade. Countries are in financial autarky, with financial assets (claims on firms, a bond, and money) only held domestically. Goods are only used for consumption, abstracting from investment. There are households, firms, a government and a central bank. There is no uncertainty, but in period 1 there may be different expectations in case of multiple equilibria.

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[9]   Also related is Bacchetta, Tille and van Wincoop (2012), who focus on the stock market rather than business cycles. Their model features self-fulfilling spikes in stock price risk and an associated sharp decline in stock prices. Bacchetta and van Wincoop (2013) extend this to an open economy framework.

[10]   Dedola and Lombardo (2012) find that that perfect co-movement is possible even with portfolio home bias. But this relies on a setup that precludes arbitrage between risky and riskfree assets as only leveraged agents hold risky assets and face borrowing constraints. As shown in van Wincoop (2013), allowing for non-leveraged agents that can conduct such arbitrage, and calibrating the relative size of leveraged institutions in financial markets, transmission is limited. The 2008 crisis saw very large arbitrage between risky and low risk assets, with a large flight to quality that increased prices of low risk Treasuries.

[11]   See Mankiw and Weinzierl (2011) or Fernandez-Villaverde et al. (2012) for recent contributions. Aghion, Bacchetta and Banerjee (2000) analyze a small open economy.

In Section 5, we examine several extensions to this benchmark model. In particular, we examine the role of investment, uncertainty and financial integration.

2.1   Households

Households make consumption and leisure decisions in both periods. Households in the Home country maximize

$$\frac{1}{1-\gamma}c_1^{1-\gamma} + \lambda l_1 + \beta\left(\frac{1}{1-\gamma}c_2^{1-\gamma} + \lambda l_2\right) \tag{1}$$

where l_t is the fraction of time devoted to leisure in period t and c_t is the period-t consumption index of Home and Foreign goods:

$$c_t = \left(\frac{c_{H,t}}{\psi}\right)^{\psi}\left(\frac{c_{F,t}}{1-\psi}\right)^{1-\psi} \tag{2}$$

where

$$c_{H,t} = \left(\int_0^{n_{H,t}} c_{H,t}(j)^{\frac{\mu-1}{\mu}}\, dj\right)^{\frac{\mu}{\mu-1}} \tag{3}$$

$$c_{F,t} = \left(\int_0^{n_{F,t}} c_{F,t}(j)^{\frac{\mu-1}{\mu}}\, dj\right)^{\frac{\mu}{\mu-1}} \tag{4}$$

Here $c_{H,t}$ is the consumption index of Home goods and $c_{F,t}$ the consumption index of Foreign goods. Consumption of respectively the Home and Foreign good j is $c_{H,t}(j)$ and $c_{F,t}(j)$. The number of Home and Foreign goods in period t is $n_{H,t}$ and $n_{F,t}$, which are equal to the number of Home and Foreign firms. The elasticity of substitution among goods of the same country is $\mu > 1$, while the elasticity of substitution between Home and Foreign goods is 1 (we examine non-unitary elasticities in Section 5). There is a preference home bias towards domestic goods as we assume $\psi > 0.5$. The specification is symmetric for the Foreign country, with the overall consumption index denoted as c_t^* and $c_{H,t}^*(j)$, $c_{F,t}^*(j)$ denoting the consumption of individual Home and Foreign goods consumption by Foreign households.

The parameter ψ captures the degree of goods market integration, with the limit of $\psi = 0.5$ reflecting perfect goods market integration. As we will see, $\psi = 0.5$ implies that in equilibrium $c_t = c_t^*$, so that financial markets are complete even though there is no asset trade.[12] This is a feature that results specifically from the Cobb-Douglas specification and is familiar from Cole and Obstfeld (1991). We can then think of $\psi = 0.5$ as perfect economic integration across the two countries.

In period 1 Home households earn labor income $W_1(1-l_1)$, where W_1 is the nominal wage rate. They also earn a dividend Π_1^C and receive a transfer of $\overline{M}_1$ in money balances from the central bank. They use these resources to consume, pay a tax T_1 to the government, buy Home nominal bonds with interest rate i and hold money balances:

$$\int_0^{n_{H,1}} P_{H,1}(j)c_{H,1}(j)dj + \int_0^{n_{F,1}} S_1 P_{F,1}(j)c_{F,1}(j)dj + T_1 + B + M_1 =$$
$$W_1(1-l_1) + \Pi_1^C + \overline{M}_1 \tag{5}$$

where $P_{H,t}(j)$ and $P_{F,t}(j)$ are the price of respectively Home and Foreign good j in the Home and Foreign currency. S_t is the nominal exchange rate in period t (Home currency per unit of Foreign currency).

In period 2 Home households earn labor income $W_2(1-l_2)$, earn a dividend Π_2^C, receive $(1+i)B$ from bond holdings, carry over M_1 in money balances from period 1, and receive an additional money transfer of $\overline{M}_2 - \overline{M}_1$ from the central bank. These resources are then used to consume, pay a tax T_2 to the government and hold money balances M_2:[13]

$$\int_0^{n_{H,2}} P_{H,2}(j)c_{H,2}(j)dj + \int_0^{n_{F,2}} S_2 P_{F,2}(j)c_{F,2}(j)dj + T_2 + M_2 =$$
$$W_2(1-l_2) + \Pi_2^C + (1+i)B + M_1 + (\overline{M}_2 - \overline{M}_1) \tag{6}$$

We assume a cash-in-advance constraint, with the buyer's currency being used for payment:

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[12]   Financial market completeness implies that the ratio of marginal utilities of consumption across the two countries is equal to the real exchange rate, which is 1 when $\psi = 0.5$.

[13]   As usual in finite-time models, there is an implicit assumption on the final use of money, e.g., agents need to return the money stock to the central bank.

$$\int_0^{n_{H,t}} P_{H,t}(j) c_{H,t}(j) dj + \int_0^{n_{F,t}} S_t P_{F,t}(j) c_{F,t}(j) dj \leq M_t \tag{7}$$

The constraint will always bind in period 2. It will bind in period 1 when the nominal interest rate i is positive. When $i = 0$, the constraint will generally not bind in period 1.

Households choose consumption and leisure to maximize (1). The first-order conditions are

$$c_1^{-\gamma} = \beta(1+i)\frac{P_1}{P_2} c_2^{-\gamma} \tag{8}$$

$$c_{H,t}(j) = \left(\frac{P_{H,t}(j)}{P_{H,t}}\right)^{-\mu} c_{H,t} \tag{9}$$

$$c_{F,t}(j) = \left(\frac{P_{F,t}(j)}{P_{F,t}}\right)^{-\mu} c_{F,t} \tag{10}$$

$$c_{H,t} = \psi \frac{P_t}{P_{H,t}} c_t \tag{11}$$

$$c_{F,t} = (1-\psi)\frac{P_t}{S_t P_{F,t}} c_t \tag{12}$$

$$\frac{W_t}{P_t} = \lambda c_t^{\gamma} \tag{13}$$

where

$$P_{H,t} = \left(\int_0^{n_{H,t}} P_{H,t}(j)^{1-\mu} dj\right)^{\frac{1}{1-\mu}}$$

$$P_{F,t} = \left(\int_0^{n_{F,t}} P_{F,t}(j)^{1-\mu} dj\right)^{\frac{1}{1-\mu}}$$

$$P_t = P_{H,t}^{\psi}[S_t P_{F,t}]^{1-\psi}$$

$P_{H,t}$ and $P_{F,t}$ are price indices of Home and Foreign goods that are denominated in respectively Home and Foreign currencies. P_t is the overall price index, denominated in the Home currency.

Equation (8) is a standard intertemporal consumption Euler equation. (9)-(10) represent the optimal consumption allocation across goods within each country. (11)-(12) represent the optimal consumption allocation across the two countries. (13) represents the consumption-leisure trade-off. As usual, the inverse of γ measures the intertemporal rate of substitution. However, in equation (13) γ also measures the wage elasticity to consumption.

There is an analogous set of first-order conditions for Foreign households. Other than for Home and Foreign prices and price indices, we only need to add * superscripts to the variables and exchange ψ and $1-\psi$. The Foreign price index is $P_t^* = (P_{H,t}/S_t)^{1-\psi} P_{F,t}^\psi$.

2.2   The Government and the Central Bank

The government and central bank policies are analogous in the two countries. We therefore again only describe the Home country. The Home government only buys Home goods. The total government consumption index is analogous to the CES index for private Home consumption:

$$g_t = \left(\int_0^{n_{H,t}} g_t(j)^{\frac{\mu-1}{\mu}} dj \right)^{\frac{\mu}{\mu-1}} \tag{14}$$

In the benchmark case we will simply set $g_t = 0$. But we will also consider a positive constant level of government spending, where $g_t = \overline{g}$. Moreover, in Section 4 we consider the role of countercyclical fiscal policy, where $g_1 = \overline{g} - \Theta(c_1 - \overline{c})$, with $\overline{c}$ consumption in the non-panic equilibrium of the model and $\Theta \geq 0$.

Optimal allocation of government spending across the different goods implies

$$g_t(j) = \left(\frac{P_{H,t}(j)}{P_{H,t}} \right)^{-\mu} g_t \tag{15}$$

We have $\int_0^{n_{H,t}} P_{H,t}(j) g_t(j) dj = P_{H,t} g_t$. Since the timing of taxation across the two periods does not matter due to Ricardian equivalence, we simply impose the balanced budget condition

$$T_t = P_{H,t} g_t \tag{16}$$

The central bank's behavior is modeled as in other two-period models (e.g., Krugman, 1998, or Mankiw and Weinzierl, 2001). The central bank credibly sets second-period money supply to stabilize second-period prices. We assume that the central bank has a zero inflation target from period 1 to period 2 so that $P_2 = P_1$. Since the cash-in-advance constraint is binding in period 2, we have $\overline{M}_2 = P_2 c_2$, and the second-period price level can be controlled through the second period money supply.

In the first period the central bank sets the nominal interest rate i. For now we will assume that the central bank sets the interest rate such that $(1+i)\beta = 1$. This corresponds to the interest rate in the flexible price equilibrium of the model. We will see that the non-panic equilibrium of the model then corresponds to the flexible price equilibrium. In Section 4 we consider what happens when during a panic the central bank lowers the interest rate to stimulate demand. Such a policy will not avert a panic when we are close to the zero-lower bound. The central bank then has limited ability to counter a business cycle decline and the equilibrium will be similar to that without any countercyclical central bank action.

2.3   Firms

The number of firms operating in period 1 is based on prior decisions and therefore taken as given. We normalize it at 1 for both countries, so $n_{H,1} = n_{F,1} = 1$. At the end of period 1 firms decide whether to continue to operate in period 2. We denote the number of period-2 firms by $n_{H,2} = n$ and $n_{F,2} = n^*$. We do not allow new firms to enter.[14]

We focus our description mainly on Home firms. Results are analogous for Foreign firms. Output of Home firm j in period t is

$$y_t(j) = (A L_t(j))^\alpha \tag{17}$$

where $L_t(j)$ is labor input, A a constant labor productivity parameter and α is between 0 and 1.

Firms set prices at the start of each period. This Keynesian assumption only bites for period 1 as no unexpected shocks happen after firms set prices at the start of period 2. For period 1 a drop in consumption during a panic lowers demand for goods and therefore production. Labor demand is then

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[14]   We could allow for entry under a fixed cost. If the fixed cost is large enough we revert to our current setup. Lower fixed costs that leads to limited entry, only partially replacing exiting firms, will only affect results quantitatively, not qualitatively.

adjusted to satisfy the demand for goods. This Keynesian aspect is critical to the self-fulfilling business cycle panic in the model.

Since prices in period 1 are preset, and their level does not matter for what follows, we simply assume that all firms set the same price of P_{H1}, so that $P_{H1}(j) = P_{H1}$. Similarly, for the Foreign firms $P_{F1}(j) = P_{H1}$. In period 2 Home firm j sets its price $P_{H,2}(j)$ to maximize profits

$$\Pi_2(j) = P_{H,2}(j) y_2(j) - \frac{W_2}{A} y_2(j)^{1/\alpha} \tag{18}$$

subject to

$$y_2(j) = c_{H,2}(j) + g_2(j) + c^*_{H,2}(j) = \left(\frac{P_{H,2}(j)}{P_{H,2}} \right)^{-\mu} \left[\psi \frac{P_2}{P_{H,2}} c_2 + g_2 + (1-\psi) \frac{S_2 P^*_2}{P_{H,2}} c^*_2 \right] \tag{19}$$

The optimal price is a markup $\mu/(\mu-1)$ over the marginal cost:

$$P_{H,2}(j) = \frac{\mu}{\mu-1} \frac{W_2}{\alpha A} y_2(j)^{\frac{1-\alpha}{\alpha}} \tag{20}$$

Second-period profits are then

$$\Pi_2(j) = \kappa \frac{1}{A} W_2 y_2(j)^{1/\alpha} \tag{21}$$

where $\kappa = [\mu(1-\alpha) + \alpha]/[(\mu-1)\alpha]$. Since all firms face the same demand and the same wage, they set the same price. From the definition of the Home price index we have $P_{H,2} = P_{H,2}(j) n^{1/(1-\mu)}$.

Bankruptcy can occur at the end of period 1. The only difference across firms in period 1 is a fixed cost. A fraction $1-\bar{n}$ of firms face an additional real cost z in period 1. This cost captures business costs other than wages.[15] Total profits of Home firm j in period 1, $\tilde{\Pi}_1(j)$, are equal to

$$\tilde{\Pi}_1(j) = \Pi_1 - P_1 z(j) = P_{H,1} y_1 - W_1 L_1 - P_1 z(j) \tag{22}$$

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[15]   We introduce firm heterogeneity to avoid the extreme case where either all or no firms go bankrupt. We choose to do so through an additive term in profits only because it simplifies the algebra. Results would not change fundamentally if

where $z(j) = 0$ for a fraction $\bar{n}$ of firms and $z(j) = z$ for a fraction $1 - \bar{n}$ of firms. It is also useful to define Π_1 as period-1 profits before paying this cost. When firm j is unable to fully pay the fixed cost, it is declared bankrupt and cannot produce in period 2. We assume that $z(j)$ does not affect aggregate resources and is paid to an agency. In case of bankruptcy, the agency seizes Π_1. The agency operates at no cost and transfers its income to households.

Since $\Pi_1 > 0$, the $\bar{n}$ firms for which $z(j)$ is zero always have positive profits in period 1 and therefore do not need to borrow to continue their operation into period 2. The other $1 - \bar{n}$ firms may need to borrow when their first-period profits are negative. But they face a maximum limit on their borrowing capacity. Let $D(j)$ be borrowing by firm j at the end of period 1. The firm then owes $(1+i)D(j)$ in period 2. It is assumed that this can be no larger than a fraction ϕ of second period profits:

$$(1+i)D(j) \leq \phi\Pi_2(j) \tag{23}$$

This standard borrowing constraint reflects that lenders can seize at most a fraction ϕ of second period profits in case of non-payment. Second-period profits are positive and known at the end of period 1.

The $1 - \bar{n}$ firms facing the cost z are fragile in that they will go bankrupt if their debt limit is insufficient to cover negative profits in period 1. This is the case when

$$\Pi_1 + \phi\frac{\Pi_2}{1+i} < P_1 z \tag{24}$$

Another way to look at the bankruptcy condition is to define the real quantity of funds π available to pay for the fixed cost:

$$\pi \equiv \pi_1 + \phi\frac{\pi_2}{1+i} \tag{25}$$

where $\pi_1 = \Pi_1/P_1$ and $\pi_2 = \Pi_2/P_2$. From (24), the $1 - \bar{n}$ fragile firms will go bankrupt when

$$\pi < z \tag{26}$$

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instead we introduced differences in firm productivity, which interacts multiplicatively with $W_1 L_1$. The binomial distribution of the cost is also assumed for analytical convenience.

Therefore the number of firms in period 2 is either 1 or $\bar{n}$, depending on whether $\pi \geq z$ or $\pi < z$.

Let D denote aggregate borrowing by firms. The total dividends received by households include dividends from firms and from the service agency. Dividends received in periods 1 and 2 are

$$\Pi_1^C = \Pi_1 + D \tag{27}$$

$$\Pi_2^C = n\Pi_2 - (1+i)D \tag{28}$$

2.4   Market Clearing

For the Home country the market clearing conditions are

$$y_t(j) = c_{H,t}(j) + g_t(j) + c_{H,t}^*(j) \quad t = 1,2 \tag{29}$$

$$n_{H,t}L_t = 1 - l_t \quad t = 1,2 \tag{30}$$

$$M_t = \overline{M}_t \quad t = 1,2 \tag{31}$$

$$B = D \tag{32}$$

These represent respectively the goods markets clearing conditions, the labor market clearing condition, the money market clearing condition and the bond market clearing condition. There is an analogous set of market clearing conditions for the Foreign country.

If we substitute into the household budget constraints (5)-(6) the bond, money and labor market clearing conditions, along with the dividend expressions (27)-(28), we get

$$P_{H,t}c_{H,t} + P_{H,t}g_t + S_t P_{F,t}c_{F,t} = \int_0^{n_{H,t}} P_{H,t}(j)y_t(j)dj \tag{33}$$

This says that national consumption is equal to GDP. The trade balance is therefore zero. Indeed, multiplying the goods market clearing condition (29) by $P_{H,t}(j)$ and aggregating and substituting into the right hand side of (33), gives the balanced trade condition

$$S_t P_{F,t}c_{F,t} = P_{H,t}c_{H,t}^* \tag{34}$$

Using the expressions for $c_{F,t}$ and $c_{H,t}^*$, this can also be written as

$$P_t c_t = S_t P_t^* c_t^* \tag{35}$$

The nominal value of consumption is equal across the two countries. This does not imply that real consumption is equal as the real exchange rate $S_t P_t^*/P_t$ is not necessarily equal to 1 when $\psi > 0.5$. Only when markets are perfectly integrated ($\psi = 0.5$) is the real exchange rate equal to 1 and $c_t = c_t^*$.

Together with the definitions of the price indices, (35) also gives an expression for relative prices that we will use below:

$$\frac{P_{H,t}}{P_t} = \left(\frac{c_t^*}{c_t} \right)^{\frac{1-\psi}{2\psi-1}} \tag{36}$$

The Foreign relative prices are the reciprocal: $P_{F,t}/P_t^* = P_t/P_{H,t}$.

2.5   Equilibrium

Appendix B provides a description of the main equilibrium conditions. Assuming $(1+i)\beta = 1$ and $g_t = 0$, the equilibrium can be reduced to a set of 6 equations in c_1, c_1^*, π, π^*, n and n^*:

$$c_1 = \frac{1}{\theta} n^{(1-\delta)\zeta} (n^*)^{\delta\zeta} \tag{37}$$

$$c_1^* = \frac{1}{\theta} n^{\delta\zeta} (n^*)^{(1-\delta)\zeta} \tag{38}$$

$$\pi = c_1 - \frac{\lambda}{A} c_1^{\gamma+1/\alpha} \left(\frac{P_1}{P_{H,1}} \right)^{1/\alpha} + \frac{\phi\beta\kappa\lambda}{A} (c_1)^{\gamma+1/\alpha} \left(\frac{P_1}{P_{H,1}} \right)^{1/\alpha} n^{-\frac{\mu}{(\mu-1)\alpha}} \tag{39}$$

$$\pi^* = c_1^* - \frac{\lambda}{A} (c_1^*)^{\gamma+1/\alpha} \left(\frac{P_1^*}{P_{F,1}} \right)^{1/\alpha} + \frac{\phi\beta\kappa\lambda}{A} (c_1^*)^{\gamma+1/\alpha} \left(\frac{P_1^*}{P_{F,1}} \right)^{1/\alpha} (n^*)^{-\frac{\mu}{(\mu-1)\alpha}} \tag{40}$$

$$n = \begin{array}{ll} \bar{n} & \text{if } \pi < z \\ 1 & \text{if } \pi \geq z \end{array} \tag{41}$$

$$n^* = \begin{array}{ll} \bar{n} & \text{if } \pi^* < z \\ 1 & \text{if } \pi^* \geq z \end{array} \tag{42}$$

where

$$\theta = \left(\frac{\lambda\mu}{(\mu-1)\alpha A} \right)^{\alpha/(1-\alpha+\alpha\gamma)}$$

$$\zeta = \frac{\alpha + \mu(1-\alpha)}{(\mu-1)(1-\alpha+\alpha\gamma)}$$

$$\delta = (1-\psi)/[(1-\alpha+\alpha\gamma)(2\psi-1)+2(1-\psi)]$$

and the relative prices depend on c_1/c_1^* as in (36).

Appendix B provides algebraic details behind these equations. Equations (37)-(38) are derived by combining the Home and Foreign counterpart of the optimal second period price setting equation (20), the labor supply schedule $W_2/P_2 = \lambda c_2^\gamma$, $P_{H,2}(j)/P_{H,2} = n^{1/(\mu-1)}$ and the consumption Euler equations (and the assumed monetary policy). Equation (39) is the expression for available funds $\pi = \pi_1 + \phi\pi_2/(1+i)$, using $W_t/P_t = \lambda c_t^\gamma$, (35) and the fact $c_2 = c_1$ from the consumption Euler equations. Equation (40) is the Foreign counterpart for available funds. After substituting the expression (36) for the relative price, available funds depend on c_1, c_1^*, n and n^*. Finally, (41)-(42) follow from the description of default in Section 2.3.

Before turning to the solution of the model, some brief comments are in order about the flexible price equilibrium, where first-period prices are perfectly flexible. We show in Appendix B that the equilibrium is then unique. This results from the absence of a Keynesian demand effect. Independent of parameters, first-period consumption is $c_1 = c_1^* = 1/\theta$, while first-period profits are $\pi_1 = \pi_1^* = [\mu(1-\alpha)+\alpha]/(\mu\theta)$. We will assume that in the flexible price equilibrium first-period profits of all firms are positive:

Assumption 1 $z < [\mu(1-\alpha)+\alpha]/(\mu\theta)$

The right hand side of the expression in Assumption 1 is equal to $\pi_1 = \pi_1^*$ in the flexible price equilibrium. We then also have $z < \pi$ since $\pi_2 > 0$, so that no firms go bankrupt ($n = n^* = 1$). Finally, we find that the equilibrium interest rates are given by $(1+i)\beta = (1+i^*)\beta = 1$. As mentioned above, this corresponds to the policy we assume in our benchmark model. The global non-panic equilibrium in the benchmark Keynesian model will then correspond exactly to the flexible price equilibrium.

3.   Multiple Equilibria and Global Panics

The model can generate multiple equilibria with either $n = 1$ (no bankruptcies) or $n = \bar{n}$ (with bankruptcies). When both equilibria exist, we call the equilibrium with bankruptcies the *panic* equilibrium as it is simply generated by low expectations. There are potentially four equilibria, characterized by the values of n and n^*. We refer to equilibria where $n = n^*$ as symmetric equilibria. The case where $n = n^* = 1$ is a global non-panic equilibrium. If in addition there is an equilibrium where $n = n^* = \bar{n}$ we refer to it as a *global panic*. But there may also be asymmetric equilibria, where only one country panics and the other does not. There are potentially two asymmetric equilibria, with either $n = \bar{n}$ and $n^* = 1$ or $n = 1$ and $n^* = \bar{n}$.

In this section we first focus on symmetric equilibria in which $n = n^*$. In that case first-period consumption, output and profits are also equal across the two countries. Then we look at equilibria when countries are in autarky, where $\psi = 1$. Finally, we consider all equilibria for any value of ψ between 0.5 and 1. We will show that when economies are in autarky ($\psi = 1$), asymmetric equilibria always exist. However, when countries are somewhat integrated, i.e., ψ is below some cutoff, there are only symmetric equilibria and a panic is necessarily global.

3.1   Symmetric Equilibria

Considering symmetric equilibria allows us to clearly illustrate the mechanism behind a global panic. Moreover, considering global panics first is natural as we will see that without a global panic equilibrium the model does not feature any type of panic equilibrium, including asymmetric panics.

The monetary policy rules $1+i = 1+i^* = 1/\beta$ imply that $c_1 = c_2$ and $c_1^* = c_2^*$ from the consumption Euler equations. Using this, it is immediate from the other equations that $n = n^*$ implies $c_1 = c_1^*$ and $\pi = \pi^*$. From (37)-(42), the equilibria are characterized by (c_1, π, n) that satisfy

$$c_1 = \frac{n^\zeta}{\theta} \tag{43}$$

$$\pi = c_1 - \frac{\lambda}{A} c_1^{\gamma+1/\alpha} + \phi\beta \frac{\mu(1-\alpha)+\alpha}{\mu\theta} n^{\zeta-1} \tag{44}$$

$$n = \begin{array}{ll} \overline{n} & \text{if } \pi < z \\ 1 & \text{if } \pi \geq z \end{array} \tag{45}$$

Substituting (43) into (44) we can write available funds π as a function of only n. Let $\pi(1)$ and $\pi(\overline{n})$ represent available funds without and with bankruptcies in the symmetric equilibrium. We will assume that parameters are such that available funds are higher without bankruptcies:

Assumption 2 $\pi(1) > \pi(\overline{n})$

This can be written in terms of a condition on the various parameters in the model.[16] A sufficient, but not necessary, condition for this to hold is that $\zeta \geq 1$, which implies $\alpha\gamma(\mu-1) \leq 1$.

Together with Assumption 1, which implies that $z < \pi(1)$, the equilibria follow directly from (43)-(45) and are summarized in the following proposition.

Proposition 1 *When Assumptions 1 and 2 hold, there are one or two symmetric equilibria. They are characterized by:*

1. $(n, c_1) = (1, 1/\theta)$ if $\pi(\overline{n}) \geq z$

2. $(n, c_1) = (1, 1/\theta)$ or $(n, c_1) = (\overline{n}, \overline{n}^\zeta/\theta)$ if $\pi(\overline{n}) < z < \pi(1)$

For the case where $\phi = 0$, so that $\pi = \pi_1$, Figure 5 illustrates the multiple equilibria in Proposition 1. The hump-shaped curve represents the first-period profits function (44). The vertical lines represent (43) for the two levels of n and the cut-off point is determined by the level of z. When $\zeta > 1$, both vertical lines cross the profit schedule when it is upward sloping. When z is in the intermediate range ($\pi(\overline{n}) < z < \pi(1)$), there are two equilibria, A and B. Equilibrium A is a good one, which we refer to as the non-panic equilibrium. First-period consumption and profits are high and no firms go bankrupt

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[16]   The condition is $\left(\overline{n}^{-\zeta} - 1\right) + \frac{1}{\kappa}\left(\overline{n}^\kappa - 1\right) + \phi\beta\left(\overline{n}^{-\zeta} - \frac{1}{\overline{n}}\right) > 0$. The condition is not satisfied for a high γ as real

wages then decline significantly during a panic, which raises profits. We will return to this issue in Section 3.5.

($n = 1$). Equilibrium B is the bad one, which we refer to as the panic equilibrium. First-period consumption and profits are low and $1 - \bar{n}$ firms go bankrupt.

The presence of two equilibria is a result of the possibility of self-fulfilling business cycle panics. This occurs due to reinforcing linkages between periods 1 and 2. The link from period 2 to period 1 is standard as low expected period 2 income leads to low period 1 consumption. The link from period 1 to period 2 operates through profits and bankruptcies. Low period 1 consumption leads to low period 1 firm profits, which leads to bankruptcies and therefore a low number of firms in period 2. This implies low period 2 income, making the belief of low period 2 income self-fulfilling.

We should be clear that this is by no means the only possible way to model the link from the present to the future. One can think of many alternatives that should deliver similar results. Low current demand may affect future output through inventory buildup, lower current investment or production chains. In addition, rather than through bankruptcy low current profits may lower future output through cost-cutting measures such as reduced R&D, less training of labor, closing some departments or branches or less investment. Finally, lower output today may reduce future output when a reduction in productive capacity is combined with sunk costs. Together with the standard link from the future to the present through expected income, these alternative mechanisms for linking the present to the future may also generate self-fulfilling beliefs.

3.2   Autarky

When $\psi = 1$ the two economies are in autarky. They only consume their own goods, so that the relative prices $P_t / P_{H,t}$ and $P_t^* / P_{F,t}$ are equal to 1 in both periods. It then follows from (37)-(42) that for each country the equilibria correspond exactly to the symmetric equilibria described above. But in autarky the equilibrium in one country has no impact on the equilibrium of another country. When $\pi(\bar{n}) < z < \pi(1)$ there are then four possible outcomes. Either country may be in the panic equilibrium B or the non-panic equilibrium A, independent of the other country. Therefore it is possible for both countries to experience a panic together, but it is also possible for just one of the two countries to experience a panic (asymmetric equilibria).

There is no a priori reason why the two countries would panic simultaneously. There may be arguments outside of the model why a panic would be global. For example, if the trigger that sets off the panic is particularly frightening, the two countries may react together. But if this trigger event takes place in the Home country,[17] it would seem odd that the Foreign country would react to it in the absence of any integration between the two countries.

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[17]   An example is the bankruptcy of Lehman Brothers or more generally events surrounding U.S. financial markets in the Fall of 2008.

3.3   When Are Panics Global?

In this section we examine all equilibria for values of ψ between 0.5 and 1. We have already described the symmetric equilibria, where $(n, n^*) = (1,1)$ or $(n, n^*) = (\overline{n}, \overline{n})$. We now need to consider asymmetric equilibria as well, where either $(n, n^*) = (\overline{n}, 1)$ or $(n, n^*) = (1, \overline{n})$. We are particularly interested in circumstances where only the two symmetric equilibria exist. When a panic occurs, it will then necessarily be global.

We will assume that symmetric multiple equilibria exist, i.e., $\pi(\overline{n}) < z < \pi(1)$ from Proposition 1. As discussed in Section 3.2, this implies that multiple equilibria also exist in individual countries in autarky. This means that asymmetric equilibria exist when $\psi = 1$. However, as we move away from autarky, i.e., as we lower ψ, the asymmetric equilibria will no longer exist, so that panics can only be global. This is stated in the following proposition.

Proposition 2 *Assume $\pi(\overline{n}) < z < \pi(1)$, so that there are multiple equilibria. There is a threshold $\psi(z) > 0.5$ such that only the symmetric equilibria exist when $\psi < \psi(z)$.*

Proof. See Appendix C.

Using (37), Figure 6 illustrates Proposition 2 by plotting all equilibrium Home consumption levels as a function of ψ. Symmetric equilibria give perfectly horizontal schedules as consumption is $c_1 = n^{\zeta}/\theta$, which is unaffected by the level of integration. This is not the case in the asymmetric equilibria. For example, a Foreign panic affects Home consumption more the greater the extent of integration (the lower ψ).

When ψ is below the threshold $\psi(z)$, only the two symmetric equilibria exist. In that case panics are necessarily global. In other words, when the level of trade is sufficiently high, or home bias sufficiently low, a panic will be perfectly coordinated across the two countries. However, the two countries do not need to be perfectly integrated. A panic will be necessarily global for all values of ψ larger than 0.5 and less than $\psi(z)$. A sufficient degree of integration, not perfect integration, is needed to guarantee that panics will be global. As we show in Section 3.5, the cutoff for ψ will generally be far above 0.5, so that we do not need to be anywhere close to full integration to assure that panics will be perfectly coordinated across countries.

Before we turn to the intuition behind this key result, it is useful to first draw out some of the implications. First, Proposition 2 implies that when the two countries are sufficiently integrated ($\psi > \psi(z)$) a panic leads to a drop in consumption that is common across countries. Consumption in

both countries drops from $1/\theta$ to $\overline{n}^{\zeta}/\theta$. Second, output drops equally in both countries and the same as consumption.[18] Third, future output is expected to drop in both countries by the same amount as well. All these pieces of evidence are consistent with the business cycle and survey data reported in Figures 1 and 3. Also consistent with the model, we can observe a worldwide decline in profits. Figure 7 shows substantial declines in profits both for the U.S. and other G7 countries.[19]

3.4   Intuition Behind Global Panics

Unless countries are perfectly integrated, business cycles shocks are only partially transmitted across countries in standard models. As we will see, this is the case in our model as well in the sense that an asymmetric panic in one country is only partially transmitted to the other country. But the key to perfect business cycle co-movement here is that under sufficient integration we can rule out asymmetric equilibria, so that a panic is necessarily global.

While we will discuss the reason for this in the context of the specifics of our model, the key point is more general. Expectation shocks in our model are self-fulfilling. When countries are sufficiently integrated it is hard to see how one country can have very negative self-fulfilling expectations about future output and income while the other country has very favorable expectations. If agents act on those beliefs, the weak country would negatively impact the strong country and the other way around, and more so the more integrated they are. Such beliefs will then not be self-fulfilling as for example income in the weak country will be favorably impacted by strong demand from the other country (with trade integration) or strong portfolio returns in the other country (with financial integration).

Returning to the specifics of our particular model, we will consider the feasibility of an asymmetric equilibrium where $n = \overline{n}$ and $n^* = 1$. Before we can determine whether such an equilibrium may exist, we first consider the impact of the Home panic on first-period consumption, output and profits in both countries.

Let $y_1 = \int_0^1 y_1(j)dj$ be aggregate Home output in period 1 (real GDP) and y_1^* aggregate Foreign output. We then have

$$c_1 = \frac{1}{\theta}\overline{n}^{(1-\delta)\zeta} \tag{46}$$

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[18]   The real value of Home output in period 1 is $P_1 c_1 / P_{H,1}$ from (33), while $P_1/P_{H,1}$ depends on c_1/c_1^* from (36) and therefore stays equal to 1. The drop in Home real GDP in period 1 is therefore the same as the drop in Home consumption. The same is the case for the Foreign country.

[19]   There is no cross-country database on aggregate corporate profits that we are aware of. The numbers in Figure 7 have been derived by aggregating profits from firms listed in the Worldscope database. We selected continuing firms over the interval and windsorized the top and bottom tails at 1 percent. The resulting profit series are divided by the GDP deflator.

$$c_1^* = \frac{1}{\theta}\bar{n}^{\delta\zeta} \tag{47}$$

and

$$y_1 = \frac{1}{\theta}\bar{n}^{(1+\delta\alpha(\gamma-1))\zeta} \tag{48}$$

$$y_1^* = \frac{1}{\theta}\bar{n}^{-\delta\alpha(\gamma-1)\zeta} \tag{49}$$

First consider output. Under autarky, where $\delta = 0$, only Home output is lower in case of Home defaults. When countries are integrated Home output is always lower than Foreign output. When $\gamma > 1$ it is even the case that Foreign output rises. So the transmission of the Home shock (lower n) to the Foreign country is either positive and partial or negative. Two factors play a role here. First, lower Home second-period income due to a lower n decreases Home consumption, which decreases demand for Foreign goods. This leads to positive but partial transmission. Second, lower Home output leads to an increase in the relative price of Home goods.[20] This leads to an expenditure switch to Foreign goods, which may actually raise Foreign output in period 1.

Consumption is equal to $c_1 = P_{H,1}y_1/P_1$ and $c_1^* = P_{F,1}y_1^*/P_1^*$. Two factors impact consumption: the change in output discussed above and the terms of trade. Similar to output, under autarky only Home consumption declines. When countries are integrated there is an additional positive transmission channel through the terms of trade, which improves for the Home country and deteriorates for the Foreign country. This raises Home consumption and lowers Foreign consumption. The overall impact is that both Home and Foreign consumption decline. But Foreign consumption declines less ($\delta < 0.5$), so that transmission is positive but partial.

We finally need to consider profits, which are critical to understanding whether asymmetric equilibria exist. We can write Home and Foreign first period profits as

$$\pi_1 = c_1 - \frac{\lambda}{A}c_1^{\gamma+1/\alpha}\left(\frac{P_1}{P_{H,1}}\right)^{1/\alpha} \tag{50}$$

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[20]   This is the case for period 1 as well as $P_1 = P_2$ and $P_1^* = P_2^*$ together imply that the terms of trade is the same in both periods.

$$\pi_1^* = c_1^* - \frac{\lambda}{A}(c_1^*)^{\gamma+1/\alpha}\left(\frac{P_1}{P_{H,1}}\right)^{-1/\alpha} \tag{51}$$

with c_1 and c_1^* as in (46)-(47) and

$$\frac{P_1}{P_{H,1}} = \overline{n}^{(1-\alpha+\alpha\gamma)\delta\zeta} \tag{52}$$

Under autarky ($\delta = 0$) we have $P_1/P_{H,1} = 1$ and only Home profits are lower due to the decline in Home consumption.[21] Trade integration impacts profits in several ways. There are three channels through which it raises Home profits and lowers Foreign profits. First, Home faces strong export demand from Foreign and Foreign faces weak export demand from Home. Second, for a given quantity of sales the increase in the relative price of Home goods raises Home real revenues and lowers Foreign real revenues. Finally, we have already seen that increased integration raises Home consumption and lowers Foreign consumption, which increases demand for Home goods and lowers demand for Foreign goods. There is one transmission channel that operates the other way. The higher relative price of Home goods leads to an expenditure switch to Foreign goods, which lowers Home profits and raises Foreign profits.

We show in Appendix C that the first three transmission channels dominate and therefore increased integration raises Home profits and lowers Foreign profits. We also show that for sufficient integration Home profits actually become larger than Foreign profits. To see why this is the case, consider $\psi \to 0.5$. When we get close to perfect integration, it follows from (46)-(47) that c_1 and c_1^* become equal. This result is familiar from Cole and Obstfeld (1991), who show that with Cobb-Douglas utility a relative change in output does not affect relative consumption due to the endogenous terms-of-trade adjustment. It then follows from (50)-(51) that Home profits only differs from Foreign profits as a result of the terms of trade, which is captured by $P_1/P_{H,1}$. We can see from (52) that $P_1/P_{H,1} < 1$, reflecting the drop in the relative price of Foreign goods. This implies from (50)-(51) that Home profits are higher than Foreign profits. More generally we show in Appendix C that Home profits is larger than Foreign profits under sufficient integration as measured by $\psi < \overline{\psi}$ for some cutoff $\overline{\psi} > 0.5$.

Based on these results, formalized in Appendix C, Figure 8 graphs Home and Foreign profits as a function of ψ. The graph captures three key points discussed above. First, under autarky ($\psi = 1$) Home profits are weaker than Foreign profits as only the Home country is affected by the Home defaults. Second, increased integration (lower ψ) raises Home profits and lowers Foreign profits. Finally, Home profits are higher than Foreign profits when ψ is below a cutoff $\overline{\psi}$.

We can only have an asymmetric panic equilibrium where $n = \bar{n}$ and $n^* = 1$ when

$$\pi_1 < z \leq \pi_1^* \tag{53}$$

In that case the fragile Home firms will indeed default ($n = \bar{n}$), while the fragile Foreign firms will not default ($n^* = 1$). Assumptions 1 and 2 imply that this is satisfied when $\psi = 1$. But it is no longer satisfied when the two countries are sufficiently integrated. It is clearly not the case when $\psi < \bar{\psi}$ as in that case Home profits are higher than Foreign profits.

More generally (53) is not satisfied for ψ less than a cutoff $\psi(z)$ that lies somewhere between $\bar{\psi}$ and 1. This is illustrated in Figure 8. When $z = z_1$, the cutoff for ψ is ψ_1. When $\psi < \psi_1$, Foreign profits are below z, so that fragile Foreign firms will default and $(n, n^*) = (\bar{n}, 1)$ cannot be an equilibrium. Similarly, when $z = z_3$, the cutoff for ψ is ψ_3. When $\psi < \psi_3$, Home profits are above z, so that fragile Home firms will not default and $(n, n^*) = (\bar{n}, 1)$ cannot be an equilibrium. The lowest possible cutoff value for ψ occurs when $z = z_2$, in which case the cutoff is $\psi = \bar{\psi}$, where Home and Foreign profits are equal. It follows that for $\psi < \psi(z)$ the asymmetric equilibria do not exist.

What is critical to Proposition 2 is not the finding that Home profits become larger than Foreign profits when $\psi < \bar{\psi}$. Rather, what is key is that Home profits rise and Foreign profits decline when countries become more integrated, which is natural with positive transmission across countries. Even if $\bar{\psi}$ were 0.5, so that Home profits is always lower than Foreign profits with limited integration, $\psi(z)$ will still be above 0.5.[22] If countries are sufficiently integrated, and therefore the difference between Home and Foreign profits becomes sufficiently small, there will generally not be an equilibrium where only Home firms go bankrupt.

Therefore only a limited amount of trade is sufficient to assure that a panic will be global in nature and therefore consumption and output move perfectly together across countries. A limited amount of trade is sufficient to either provide enough stability to the Home country, avoiding a panic altogether, or to drag the Foreign country down into a panic as well. A self-fulfilling shock to expectations cannot just occur in one country if the countries are sufficiently integrated. The countries necessarily suffer a common fate.

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[21]   This requires Assumption 2.

[22]   The only exception is the knife-edge case where $z = z_2$.

3.5   Numerical Illustration

While the model is obviously highly stylized, it is still useful to provide a numerical illustration for reasonable levels of parameters. We will set the elasticity μ equal to 3. Broda and Weinstein (2006) estimate this elasticity using 8-digit, 5-digit and 3-digit industry levels. In all cases they find that the median elasticity across industries is just below 3. We set $\alpha = 0.75$. This delivers a labor share of $\alpha(\mu-1)/\mu = 0.5$, which is consistent with 2010 data for the U.S., Japan and the Euro zone on the ratio of employee compensation to GDP. We normalize private consumption in the non-panic state to be 1 by setting λ/A such that $\theta = 1$. We re-introduce government spending, which was only suppressed in the previous subsections for analytic tractability. We set $g_t = \overline{g} = 0.3$ in both periods, implying that government consumption as a fraction of GDP is 0.3/1.3=0.23. This is consistent with recent data from industrialized countries for government spending (consumption plus investment) relative to GDP. For now we set $\phi = 0$, so that the borrowing constraint is very tight: firms cannot borrow at all. We will investigate the role of borrowing constraints further in the next section.

The only parameter left is γ. It is hard to calibrate as it plays three roles in the model: rate of risk aversion, inverse of intertemporal elasticity of substitution and real wage cyclicality. The real wage is λc^{γ}. Based on estimates of risk-aversion and the intertemporal elasticity of substitution γ should be larger than 1. But this is inconsistent with the evidence that the average real wage rate is not very cyclical. Moreover, given realistic choices for the other parameters the model implies counterintuitively that $\pi(1) < \pi(\overline{n})$ when γ is set at 1 or larger. The reason is that in the panic state the real wage is much lower, which raises firm profits. In order to avoid this strong cyclicality of the wage rate, we consider results both for the case where γ is well below 1 and the extension where nominal or real wages are rigid (preset at the start of each period). This extension is straightforward and described in Appendix D.

When we set $\gamma = 0.2$, so that the real wage rate is not very cyclical, we find $\overline{\psi} = 0.9$, independent of the level of $\overline{n}$. The actual cutoff $\psi(z)$ then lies somewhere between 0.9 and 1. Only limited trade is then sufficient to guarantee a global panic. When 10% of private consumption goods are imported a panic is necessarily global and therefore business cycles will be perfectly synchronized during the panic. $\overline{\psi}$ will be only slightly lower, at 0.88, when we set γ infinitesimally close to 0, so that the real wage rate is not cyclical at all.

As discussed further in Appendix D, under both nominal and real wage rigidity wages are set at the start of each period under the assumption that there will be no panic.[23] Results will be very similar when setting the probability of a panic at a small positive number. This does not affect period 2 as

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[23]   Even though firms preset their prices, there is a difference between nominal and real wage rigidity due to the exchange rate impact on the price level.

there are no further unexpected shocks during period 2. When the real wage is negotiated at the start of period 1, it will then be set at its equilibrium non-panic level. When instead the nominal wage rate is agreed to in advance, the real wage will be equal to the non-panic real wage rate times $\overline{P_1}/P_1$, where $\overline{P_1}$ is the price index without a panic. We now set γ at 3, which is a standard value when measuring risk aversion or the inverse of the intertemporal elasticity of substitution.

Under real wage rigidity we find that $\overline{\psi}$ is 0.89. Note that this is not the same model as under flexible real wages with γ very small since the second period equilibrium does depend on γ. Nonetheless the result is virtually identical and it again does not depend on $\overline{n}$. Under nominal wage rigidity $\overline{\psi}$ is a bit lower at 0.77, so that $\psi(z)$ is in the range of 0.77 to 1. But it is still the case that limited trade is needed to guarantee perfect synchronization of panics across countries. It is sufficient that 23% of private consumption goods are imported. This number may be even less depending on the precise value of z.[24]

We can also numerically evaluate the extent of traditional business cycle transmission associated with asymmetric shocks. Since there are no exogenous asymmetric shocks in the model, we consider transmission associated with an asymmetric panic. Take the example of real wage rigidity where $\overline{\psi} = 0.89$. Assume that $\psi(z) = \overline{\psi}$ and that $\psi = 0.9 > \overline{\psi}$. We are then in the region where asymmetric panics are possible. Using the parameter values discussed above, the drop in log Foreign consumption is then only a fraction 0.05 of the drop in log Home consumption. Transmission is positive but small. Since $\gamma > 1$, (49) implies that Foreign output rises in this case, so that transmission to Foreign output is negative. But only slightly more trade integration (ψ equal to 0.89 or less) guarantees that panics are global, allowing us to explain the perfect business cycle synchronization while retaining significant home bias as seen in the data.

4.   Vulnerabilities

We can now consider factors that make countries vulnerable to self-fulfilling panics. We focus on symmetric equilibria. If symmetric panics do not exist, no type of panic, including asymmetric ones, exist in the model. We consider a version of the model that is general enough to focus on the role of credit, monetary policy and fiscal policy. These are captured by respectively ϕ, i and g_t. At the

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[24]   The slightly lower cutoff under nominal wage rigidity can be explained as follows. We have seen that when a panic is limited to the Home country, Home profits rise and Foreign profits decline as we lower ψ, until they are equal at $\psi = \overline{\psi}$. But the decrease in the relative price of Foreign goods will lower the Home price index and more so the higher the level of trade (the lower ψ). When the nominal wage rate is fixed, this by itself raises the real wage rate and lowers Home profits as we lower ψ. It will remain the case, as a result of the other channels that we discussed, that Home and Foreign profits are equal for a value $\overline{\psi}$ larger than 0.5, but this counterweigting force reduces somewhat the value of $\overline{\psi}$.

same time we will simplify by setting $\zeta = \alpha = 1$. This leads to a cleaner set of equilibrium equations, but is not critical to the results. As shown in Appendix B, the schedules that determine the symmetric equilibrium are then

$$c_1 = [\beta(1+i)]^{-1/\gamma} \frac{n}{\theta} \tag{54}$$

$$\pi = c_1 + g_1 - \frac{\lambda}{A} c_1^{\gamma}(c_1 + g_1) + \frac{\phi}{(1+i)\mu\theta}\left(1 + \frac{g_2\theta}{n}\right) \tag{55}$$

$$n = \begin{matrix} \overline{n} & \text{if } \pi < z \\ 1 & \text{if } \pi \geq z \end{matrix} \tag{56}$$

We consider different versions of this set of equilibrium equations, dependent on the vulnerability of interest. We can think of $\phi = 0$, $g_t = 0$ and $(1+i)\beta = 1$ as a benchmark that we deviate from one parameter at a time.

4.1   Credit

In order to consider the role of credit we focus on the impact of the parameter ϕ, while setting $\beta(1+i) = 1$ and $g_t = 0$. Equilibrium is then characterized by two schedules:

$$c_1 = \frac{n}{\theta} \quad \text{with } n = \overline{n} \text{ if } \pi < z \text{ and } n = 1 \text{ if } \pi \geq z \tag{57}$$

$$\pi = c_1 - \frac{\lambda}{A} c_1^{1+\gamma} + \frac{\phi\beta}{\mu\theta} \tag{58}$$

These schedules are shown in Figure 9 for two values of ϕ. The vertical lines represent the consumption schedule while the humped shaped line reflects the available fund schedule. A higher ϕ raises the available fund schedule. Figure 9 shows that when ϕ is low, so that credit is tight, there may be two equilibria, so that self-fulfilling panics are possible. But when credit is loose, so that ϕ is high, only the non-panic equilibrium exists. The more firms are able to borrow, the less fragile they are. They are then better able to withstand a drop in demand that lowers first-period profits. This in turn can make a self-fulfilling panic impossible. While it remains the case that conditions in period 2 affect consumption in period 1, the linkage in the other direction is broken under loose credit conditions. Even with low consumption in period 1, leading to low profits, firms can avoid bankruptcy by borrowing.

4.2   Monetary Policy

So far we have assumed that monetary policy is a zero inflation policy and $(1+i)\beta = 1$, so that the non-panic equilibrium corresponds to the flexible price equilibrium. But it is sensible for the central bank to lower the interest rate when faced with a panic that reduces output and consumption. However, the central bank may be constrained by the zero lower bound. We will now assume that $\phi = 0$ and $g_t = 0$, but we no longer restrict monetary policy to be $(1+i)\beta = 1$. The symmetric equilibrium is then determined by

$$c_1 = [\beta(1+i)]^{-1/\gamma}\frac{n}{\theta} \quad \text{with } n = \bar{n} \text{ if } \pi < z \text{ and } n = 1 \text{ if } \pi \geq z \qquad (59)$$

$$\pi = c_1 - \frac{\lambda}{A}c_1^{1+\gamma} \qquad (60)$$

The interest rate only enters the consumption schedule. Lowering the interest rate shifts the consumption schedule to the right.

Now consider the following policy. In the absence of a panic the central bank keeps $(1+i)\beta = 1$, so that we achieve the flexible price equilibrium. But when a panic occurs the central bank lowers the interest rate. The chart on the left-hand side of Figure 10 considers the case where the central bank lowers the interest rate all the way to zero during a panic. When β is only slightly below 1, so that the non-panic interest rate $i = \bar{i} = 1 - 1/\beta$ is already close to zero, this involves only a small rightward shift of the left vertical line of the consumption schedule. We see that in that case the central bank cannot avoid a panic due to the zero lower bound. There is a panic equilibrium at B' that is quite close to the panic equilibrium B under the passive policy $(1+i)\beta = 1$. The reason for this is that the central bank does not have much room to maneuver when the interest rate is already close to 0.

When instead β is well below 1, so that we are far from the zero lower bound without a panic, the interest rate can be lowered much more during a panic. This leads to a larger rightward shift of the left vertical line of the consumption schedule. When the central bank follows this policy, it is clear from Figure 10 that a panic can be avoided altogether. A large drop in the interest rate leads to a significant rise in first period consumption, which dampens the decline in firm profits and thus avoids defaults.

The chart on the right hand side of Figure 10 illustrates this point as well. We can think of (59) as a downward sloping IS curve in the space of (i, c_1). A panic lowers n, which shifts the IS curve to the left. When policy is passive, so that $i = 1 - 1/\beta$, the panic leads to a significant drop in first-period consumption. We shift from point A to point B, corresponding to the same points in the chart on the

left. If instead the central bank lowers the interest rate to zero during the panic, we move to point B'. The chart is drawn for the case where β is only slightly below zero, so that the interest is already close to zero without a panic. Lowering the interest further, all the way to zero, will then not raise consumption very much. Profits will then remain very weak and we are unable to escape bankruptcies and therefore the panic.

There is another policy option that theoretically exists and allows the central bank to avoid a panic even when close to the zero lower bound. Instead of a zero inflation policy it could adopt a high inflation policy during a panic. The consumption schedule is then

$$c_1 = [\beta(1+i)\frac{P_1}{P_2}]^{-1/\gamma}\frac{n}{\theta} \quad \text{with } n = \bar{n} \text{ if } \pi < z \text{ and } n = 1 \text{ if } \pi \geq z \tag{61}$$

High inflation expectations would then lead to a large rightward shift of the left vertical line of the consumption schedule in the left chart of Figure 10. The panic equilibrium would then no longer exist. This policy has been widely discussed but suffers from a credibility problem as ex-post the central bank has little incentive to generate the promised inflation.[25]

4.3   Fiscal Policy

Figure 11 illustrates the role of fiscal policy. In this case we set $\phi = 0$ and $(1+i)\beta = 1$, so that the two schedules become

$$c_1 = \frac{n}{\theta} \quad \text{with } n = \bar{n} \text{ if } \pi < z \text{ and } n = 1 \text{ if } \pi \geq z \tag{62}$$

$$\pi = c_1 + g_1 - \frac{\lambda}{A}c_1^{\gamma}(c_1 + g_1) \tag{63}$$

First consider the case where fiscal policy takes the form $g_1 = \bar{g}$, which is illustrated in the left chart of Figure 11. A higher level of $\bar{g}$ then shifts upward the available funds schedule.[26] The chart illustrates that when government consumption is sufficiently high, the panic equilibrium is ruled out. Only the non-panic equilibrium without bankruptcies exists. With a very high level of government consumption, it is impossible to have a self-fulfilling business cycle panic because government

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[25]   Such credibility issues cannot be properly analyzed in our model as there is no cost of inflation.

[26]   The derivative of π with respect to $\bar{g}$ is $1 - (\lambda/A)c_1^{\gamma}$. When $c_1 = 1/\theta$, as in the non-panic equilibrium, this derivative is $1/\mu$, which is positive. Only for first-period consumption values well above that can the derivative be negative, but those are not of interest to us as first period consumption can be no larger than $1/\theta$.

spending is not affected by expectations. Even if private consumption were to decline substantially, period-1 profits would remain relatively strong because of the stable government spending. This precludes the fragile firms from going bankrupt, thus avoiding a self-fulfilling panic.

The chart on the right hand side considers the role of countercyclical fiscal policy. The broken humped shaped schedule assumes that fiscal policy takes the form $g_1 = \bar{g} - \Theta(c_1 - 1/\theta)$. In that case government consumption is the same as under the $g_1 = \bar{g}$ policy in the absence of a panic. But when a panic occurs, which lowers first period consumption, government spending is higher. When fiscal policy is sufficiently countercyclical, as measured by the parameter Θ, the chart shows that the panic equilibrium no longer exists. When the drop in private consumption during a panic is sufficiently offset by an increase in government consumption, firm profits remain relatively strong and bankruptcies are avoided.

4.4   Vulnerabilities during the 2008 Crisis

There are three ways in which the world economy was particularly vulnerable to a self-fulfilling panic in 2008. First, credit was known to be tight due to large losses experienced by banks and other financial institutions since early 2007, leading to deleveraging in the financial system. Second, interest rates around the world were close to zero even prior to the Fall of 2008, leaving central banks little room to maneuver. Third, the Great Recession took place against the backdrop of high levels of government debt, which limited the ability of fiscal authorities to respond with strong countercyclical policies.[27] Moreover, several countries had adopted fiscal rules, also limiting the flexibility of fiscal policy. These three factors were combined with increased global economic integration in recent decades, which made the world particularly vulnerable to a globally synchronized rather than a local panic.

5.   Extensions

In this section we consider four extensions to the benchmark model. While these extensions make the model more realistic, they do not alter the main results derived in the benchmark case. The first extension introduces international risk sharing, which leads to further integration across the two countries. The second extension allows for a non-unitary elasticity of substitution between Home and Foreign goods. The third extension adds investment and is able to explain a synchronized drop in investment as observed during the Great Recession. The last extension adds uncertainty about z. A panic then also leads to an increase in uncertainty about future output that is common across countries, consistent with what we saw during the Great Recession as documented in Figure 3.

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[27]   Even before fiscal debt around the globe rose significantly as a result of the recession itself, gross public debt as a percent of GDP stood close to 80% among advanced economies (see for example the World Economic Outlook, International Monetary Fund, October 2012). With the exception of the end of World War II, this is the highest level in over a century.

5.1   Financial Integration

In the model so far the two countries trade goods but are in financial autarky. We have seen that a limited degree of goods market integration is sufficient to guarantee that a business cycle panic is global. We now add to this financial integration. We only consider the extreme case of full risk sharing.[28]

There is room for risk sharing as business cycle panics are shocks that may be limited to one country. Under complete markets the ratio of marginal utilities of consumption is equal to the real exchange rate:

$$\frac{c_t^{-\gamma}}{(c_t^*)^{-\gamma}} = \frac{P_t}{S_t P_t^*}$$

(64)

This replaces the condition $P_t c_t = S_t P_t^* c_t^*$ under financial autarky. As long as γ is different from 1 these two conditions will differ.[29] The expression (36) for relative prices no longer holds and is replaced by (64). This is the only change to the model. The equations (68)-(75) in Appendix B that summarize the equilibrium all remain the same, but the relative prices $P_{H,t}/P_t$ and $P_{F,t}/P_t^*$ that enter these equations are now based on (64).[30]

We find numerically that risk sharing tends to further increase the cutoff level of ψ below which a panic is necessarily global. With financial integration, less trade integration is then needed to assure a global panic. For example, in the numerical exercise in Section 3.5 we found that $\overline{\psi}$ was 0.89 under real wage rigidities and 0.77 under nominal wage rigidities.[31] With risk sharing these numbers increase to respectively 0.95 and 0.84.

To understand the role of risk sharing, consider again the case where only the Home country panics, so that $(n, n^*) = (\overline{n}, 1)$. Under risk sharing, and assuming that $\gamma > 1$, there will be a net transfer to Home when it is hit by a panic. This leads to an increase in relative demand for Home goods, which further raises the relative price of Home goods. The Home terms-of-trade improvement will then be

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[28]   Intermediate cases with partial financial integration can be accomplished in many ways and this is not necessarily captured well through one parameter in a way that is analogous to ψ for goods market integration.

[29]   We assume that only households share risk. Firms do not have access to risksharing because of standard principal agents problems that also lead to borrowing constraints.

[30]   We have $P_t/P_{H,t} = (c_t/c_t^*)^{\gamma(1-\psi)/(2\psi-1)}$ and $P_t^*/P_{F,t} = P_{H,t}/P_t$.

[31]   As explained, without wage rigidities we needed to set γ close to zero to avoid excessive wage cyclicality, which is particularly unrealistic in the present context of risksharing where γ plays a role as the rate of relative risk-aversion. With wage rigidities we set $\gamma = 3$.

even larger than without risk sharing. The favorable impact of this terms-of-trade improvement on Home profits was discussed in Section 3.4. This implies that as ψ decreases below one, Home profits increase and Foreign profits decrease more than before. Therefore, the two profit schedules meet each other at a higher level of $\overline{\psi}$ in Figure 8. A panic limited to only one country is therefore less likely in equilibrium.

5.2   Elasticity of Substitution

Throughout the paper so far we have assumed a unitary elasticity of substitution between Home and Foreign goods. We now relax this assumption by adopting a CES specification with an elasticity of substitution of ν between Home and Foreign goods:

$$
c_t = \left[\psi^{1/\nu} c_{H,t}^{\frac{\nu-1}{\nu}} + (1-\psi)^{1/\nu} c_{F,t}^{\frac{\nu-1}{\nu}} \right]^{\frac{\nu}{\nu-1}}
\tag{65}
$$

The specification for c_t^* is analogous, with the weights ψ and $1-\psi$ switched.

As was the case for risk sharing, equations (68)-(75) in Appendix B that describe the equilibrium of the model remain unchanged. The only change again applies to the expression for relative prices that enter these equations. Relative prices are derived from the balanced trade condition $S_t P_{F,t} c_{F,t} = P_{H,t} c_{H,t}^*$. With a unitary elasticity this implies $P_t c_t = S_t P_t^* c_t^*$. With an elasticity ν this generalizes to

$$
\left(\frac{S_t P_{F,t}}{P_{H,t}} \right)^{\nu-1} \left(\frac{S_t P_t^*}{P_t} \right)^{\nu} = \frac{c_t}{c_t^*}
\tag{66}
$$

The left hand side is a function of the relative price $S_t P_{F,t}/P_{H,t}$, so this gives an implicit solution of the relative price as a function of c_t/c_t^*.[32]

We find numerically that the cutoff $\psi(z)$ rises when we lower ν below 1 and falls when we raise ν above 1. There is evidence that ν is in fact lower than 1. For example, Hooper, Johnson and Marquez (2000) estimate import price elasticities to be well below 1 for the G-7 countries. Using the parameter assumptions from Section 2.5 we find that lowering ν from 1 to 0.7 raises $\overline{\psi}$ from 0.91 to 0.95 for the flexible wage case, from 0.9 to 0.95 for the rigid real wage case and from 0.77 to 0.89 for

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[32]   It is well known that for sufficiently low elasticities of substitution (in our case below 0.5), this balanced trade condition has more than one solution for the relative price. This is an entirely separate form of multiplicity, discussed for example by Bodenstein (2010).

the case of rigid nominal wages. These results imply that with trade elasticities less than 1 even less trade is needed to guarantee that panics will be global in nature.

As discussed in Section 3.4, when only the Home country panics the only negative impact of trade on Home profits operates through the expenditure switching effect. The higher relative price of Home goods leads to a substitution from Home to Foreign goods. But this effect is weakened when the price elasticity is less than 1. The result is that Home profits rises even more with higher trade integration (lower ψ) and Foreign profits drops more. This raises $\overline{\psi}$ in Figure 8 and raises the cutoff $\psi(z)$ below which panics are necessarily global events.

5.3   Investment

As shown in Figure 1, investment also declined sharply during the Great Recession. And the decline was again of similar magnitude in the rest of the world as in the United States. To capture this, we now consider a simple extension that allows for investment.

We assume that firms that do not go bankrupt need to invest in period 1 in order to operate in period 2. To simplify, we assume a given level of required investment per firm of $\overline{k}$. This investment is measured as the same index of Home and Foreign goods as for consumption. Investment demand for individual goods therefore takes the same form as for consumption, with c_1 replaced by I_1 and c_1^* by I_1^*. Aggregate investment is $I_1 = n\overline{k}$ and $I_1^* = n^*\overline{k}$.

The equilibrium conditions (68)-(75) listed in Appendix B remain the same with two exceptions that affect the available funds schedule. First, investment $\overline{k}$ needs to be subtracted from first period profits. Second, c_1 and c_1^* need to be replaced by $c_1 + I_1$ and $c_1^* + I_1^*$ (with the exception of wages, which only depend on consumption as in (13)). The only other change is to the expression for the relative price in period 1. It is derived from the balanced trade condition. Without investment we showed that it can be written as $P_1 c_1 = S_1 P_1^* c_1^*$. With investment it becomes $P_1(c_1 + I_1) = S_1 P_1^*(c_1^* + I_1^*)$. Correspondingly, in the expression (36) for the period-1 relative price we again need to replace c_1 and c_1^* with $c_1 + I_1$ and $c_1^* + I_1^*$.

The change in the expression for the relative price makes it more difficult to derive analytical results, but the numerical results are consistent with Propositions 1 and 2. If we set $\overline{k}$ such that the ratio of investment to GDP is 0.15 without a panic (the average for the U.S. since 1990), and set the other parameters the same as in Section 3.5, the values of $\overline{\psi}$ remain virtually the same. Therefore it is again the case that limited integration is sufficient to assure that a panic is global. The only difference is that now during a global panic there is also a synchronized drop in investment in both countries.

Another interesting point relates to the Paradox of Thrift. All agents in the economy attempt to save more because of an anticipated drop in future income. But in the end equilibrium saving will be lower around the world. This occurs because the increase in desired saving leads to a drop in demand in period 1, which lowers output and income in period 1. For intertemporal smoothing reasons this reduces period 1 saving. In the model without investment equilibrium saving will remain unchanged at zero during a global panic. But since we now have an endogenous decline in investment during the panic, global saving must have declined as well. This is consistent with the data, which show a decline in global saving and investment during the 2008-2009 crisis.

5.4   Uncertainty

A simple way to introduce uncertainty is to assume that the level of the fixed cost z is not known in advance. Let us assume that z can take the values z_L or z_H, with $z_H > z_L > 0$. The probability of either value is 0.5 and the draw is uncorrelated across countries. As we will see, this generates business cycle uncertainty only when there is a panic, consistent with the evidence of a significant spike in GDP uncertainty during the Great Recession, documented in Figure 3.

Of the equilibrium conditions (68)-(75) listed in Appendix B, only the consumption Euler equations will change. Previously period 2 consumption was known in period 1, while now it may be uncertain. Assuming $\phi = 0$, the Home fragile firms default when $\pi_1 < z$. This depends on the level of z. We assume that the fixed cost is paid at the end of period 1 and is unknown when consumption decisions are made.

Let p_D be the probability of default. We have $p_D = 0$ when $\pi_1 \geq z_H$, $p_D = 1$ when $\pi_1 < z_L$ and $p_D = 0.5$ when $z_L \leq \pi_1 < z_H$. In the latter case, default will depend on whether the draw of z is z_L or z_H. The probability of default p_D^* in the Foreign country depends similarly on π_1^*.

Let $c_2(n, n^*)$ and $c_2^*(n, n^*)$ be second-period consumption in both countries as a function of the number of firms. This takes the form, $c_2 = \frac{1}{\theta} n^{(1-\delta)\zeta} (n^*)^{\delta\zeta}$ when $g_2 = 0$ but more generally is derived from (68)-(69) in Appendix B. There are now 4 possible outcomes, dependent on whether or not there is default in Home and Foreign. This leads to the following consumption Euler equation for Home (assuming $(1+i)\beta = 1$):

$$
\begin{aligned}
c_1^{-\gamma} = &\, p_D p_D^* c_2(\bar{n}, \bar{n})^{-\gamma} + (1-p_D)(1-p_D)c_2(1,1)^{-\gamma} + \\
&\, p_D(1-p_D^*)c_2(\bar{n},1)^{-\gamma} + (1-p_D)p_D^* c_2(1,\bar{n})^{-\gamma}
\end{aligned}
\tag{67}
$$

The Foreign consumption Euler equation is analogous.

We can numerically verify the equilibria by considering all 9 possible values of the pair (p_D, p_D^*). Given a set of values for these default probabilities, we can compute first-period consumption from the consumption Euler equations. This gives us expressions for first-period profits in both countries, which maps into values of p_D and p_D^* as described above. When the latter are consistent with their assumed values, there is an equilibrium.

To provide an illustration of the type of equilibria that this can generate, consider again the parameter values in Section 3.5. Let $z_L = 0.5$ and $z_H = 0.58$. In the case of rigid real wages we find that for $\psi < 0.92$ there are two equilibria. In one equilibrium there is no panic in either country. Consumption and profits are high and the probability of default is zero. In the second equilibrium there is a panic. Consumption and profits are weak. The probability of default is 0.5 as there will not be default when $z = z_L$. The panic is synchronized across the two countries. When $\psi > 0.92$ these same two equilibria still exist. In addition there are now mixed equilibria where only one country panics, with a 0.5 probability of default, and the other does not.

The basic difference relative to the previous equilibria is that in a panic equilibrium there is now a positive probability of default rather than certain default. The main result of the paper still holds in that a limited extent of trade integration ($\psi < 0.92$) is sufficient to guarantee that panics are global. The same equilibria also apply to nominal wage rigidities, with the cutoff for ψ being 0.83, as well as flexible wages.[33]

Business cycle uncertainty is now endogenous and only spikes during a panic. Without a panic, consumption and profits are strong. No firms default, whether $z = z_L$ or $z = z_H$. The exogenous uncertainty about z therefore does not generate output uncertainty. In a panic, however, consumption and profits are weak. In that case the value of z does matter. When $z = z_L$ defaults can still be avoided even though profits are weak. But when $z = z_H$ the fragile firms will default. Therefore the uncertainty about z translates into output and consumption uncertainty only during a panic.

The endogenous uncertainty also contributes to the self-fulfilling mechanism itself. Without uncertainty we saw that the self-fulfilling beliefs operate through the expected level of second period income. Lower expected income leads to lower consumption, which causes lower profits that generates bankruptcies that are consistent with the belief of lower expected future income. With uncertainty the second moment plays a role as well.[34] Higher income uncertainty leads to lower consumption as a

---

[33]   In the case of flexible wages we need to set different values for z_L and z_H. For example, if we set them at 0.4 and 0.54 the same types of equilibria occur, with the cutoff for ψ being 0.92.

[34]   See Basu and Bundick (2012) for an analysis of the the impact of exogenous uncertainty in a sticky-price model. Ravn and Sterk (2012) focus on the impact of job uncertainty.

result of precautionary saving. This in turn lowers profits, which makes the fragile firms more sensitive to fixed cost shocks. This generates uncertainty about defaults, making the belief of income uncertainty self-fulfilling.

It is also useful to note that panics do not necessarily imply bankruptcies in this extension. When $z_L \leq \pi_1 < z_H$ in a panic, bankruptcies only occur when $z = z_H$. It is the increased expectation of bankruptcies and uncertainty about bankruptcies that drives the panic. But dependent on z, these bankruptcies may not necessarily materialize. Moreover, since z and z^* are uncorrelated, bankruptcies may occur in only one country, even when the panic is global. In other words, perfect co-movement may only occur in a global panic and not in subsequent periods.

6.   Conclusion

The paper is motivated by evidence of close business cycle co-movement during the Great Recession. Even though the housing and financial shock originated in the United States, business cycles in the rest of the world were impacted to a similar extent. Given limited trade and financial integration across countries this is surprising as standard models with exogenous shocks and limited integration generate only partial transmission. It is also surprising given the much lower co-movement of business cycles during prior recessions.

To explain this we have developed a two-country model with self-fulfilling business cycle panics. The self-fulfilling mechanism is a result of a circular relationship between present and future macroeconomic conditions. The link from the future to the present is standard in almost any intertemporal model as lower expected future income lowers consumption today. We have modeled the link from the present to the future through profits and bankruptcies, with lower demand today leading to weaker profits, which increases bankruptcies and lowers future output. But many other possible mechanisms may generate such a link from the present to the future.

We have shown that the model is consistent with high international co-movement observed during the Great Recession. We find that limited economic integration is sufficient to assure that a panic, when it occurs, is necessarily perfectly synchronized across countries. In a panic, consumption, investment, and output collapse similarly across countries. Moreover, perceived uncertainty increases equally across countries.

At the same time we shed light on the fact that such strong business cycle co-movement as seen during the Great Recession is historically unusual. We have argued that several factors made the 2008 episode particularly vulnerable to such a global panic: tight credit, very low interest rates, rigid fiscal policy, combined with increased economic integration across countries. And of course there was an unusually strong trigger event for a panic in the form of U.S. financial market turmoil. The combination of these conditions separates the 2008 episode from previous recessions.

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Figure 1. Global Growth (Percent; Annual; Real)*
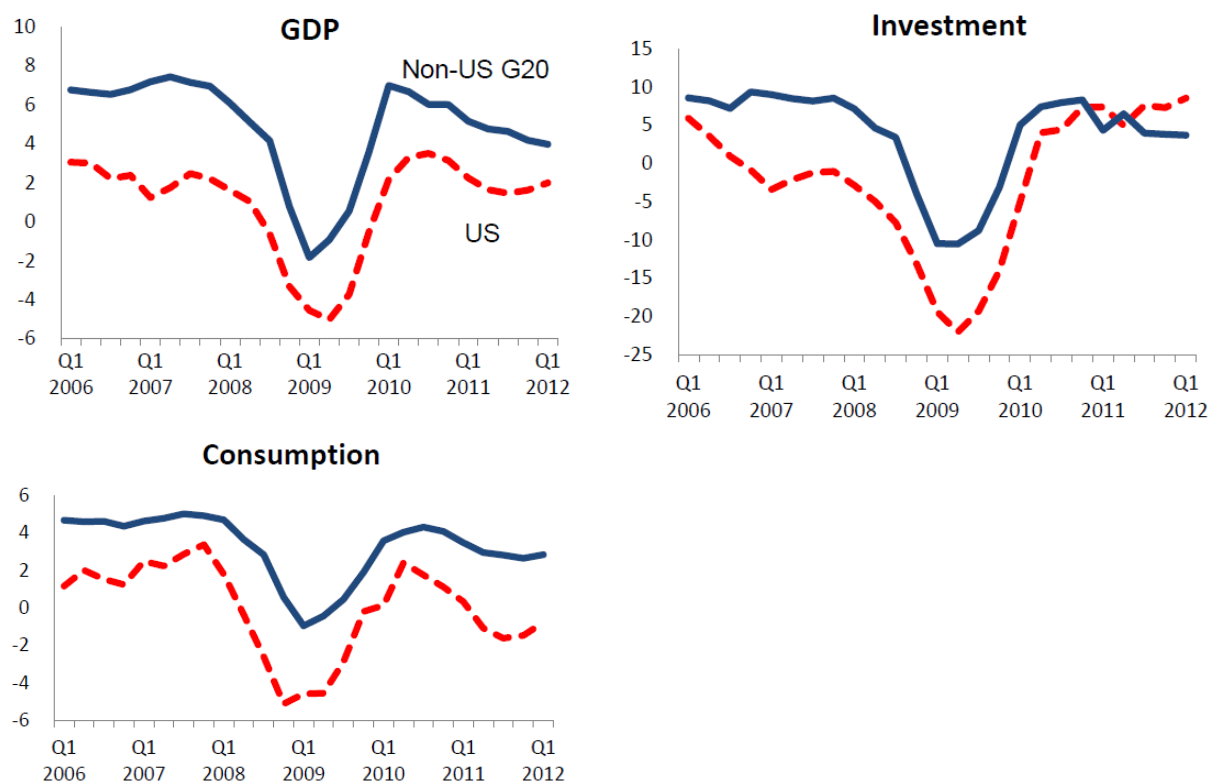
* Source: Datastream. Growth over past 4 quarters. Broken line is the U.S.; solid line is the non-U.S. G20 minus Saudi Arabia. Consumption and investment also do not include China.

Figure 2. Real GDP Growth During the Great Depression
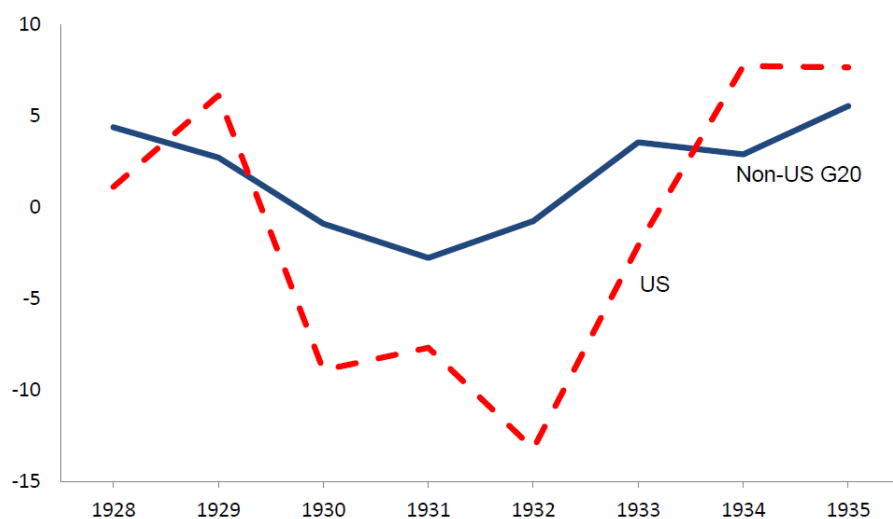
* Source: Angus Maddison. Broken line is the U.S.; solid line is the non-U.S. G20 minus Saudi Arabia minus South Africa.

Figure 3. GDP Growth Forecasts Probabilities: Expectation and Variance*
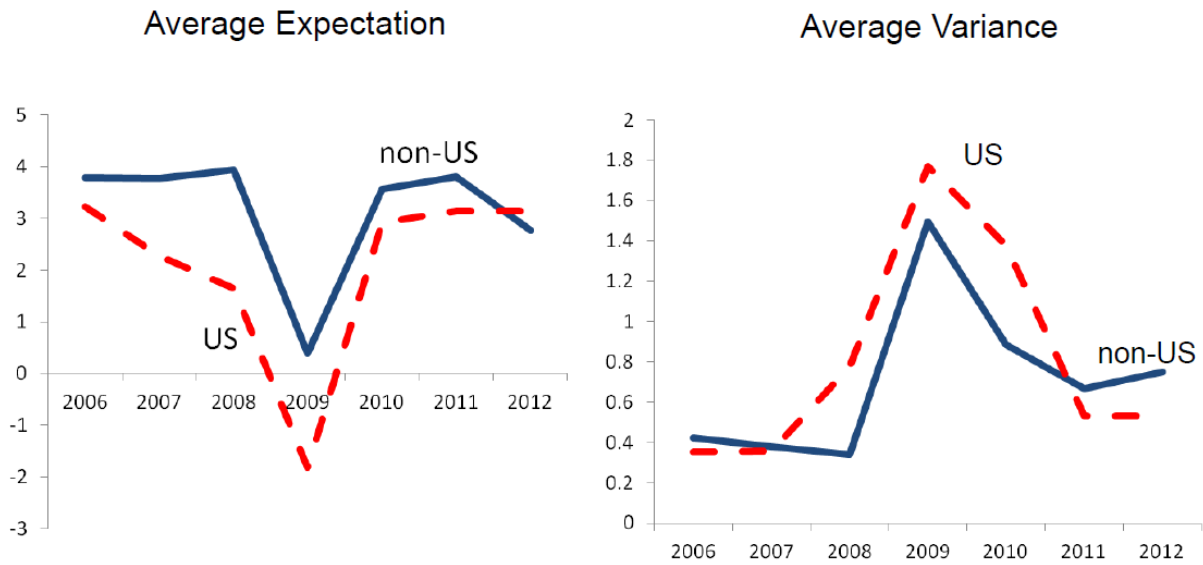
* Data from Consensus Forecasts, based on one-year ahead forecast probabilities. See Appendix A for a description. Non-US: Australia, China, Hong Kong, India, Indonesia, Malaysia, New Zealand, Singapore, South Africa, Taiwan, Thailand, Japan, Germany, France, U.K., Italy, Canada

Figure 4. Total Credit
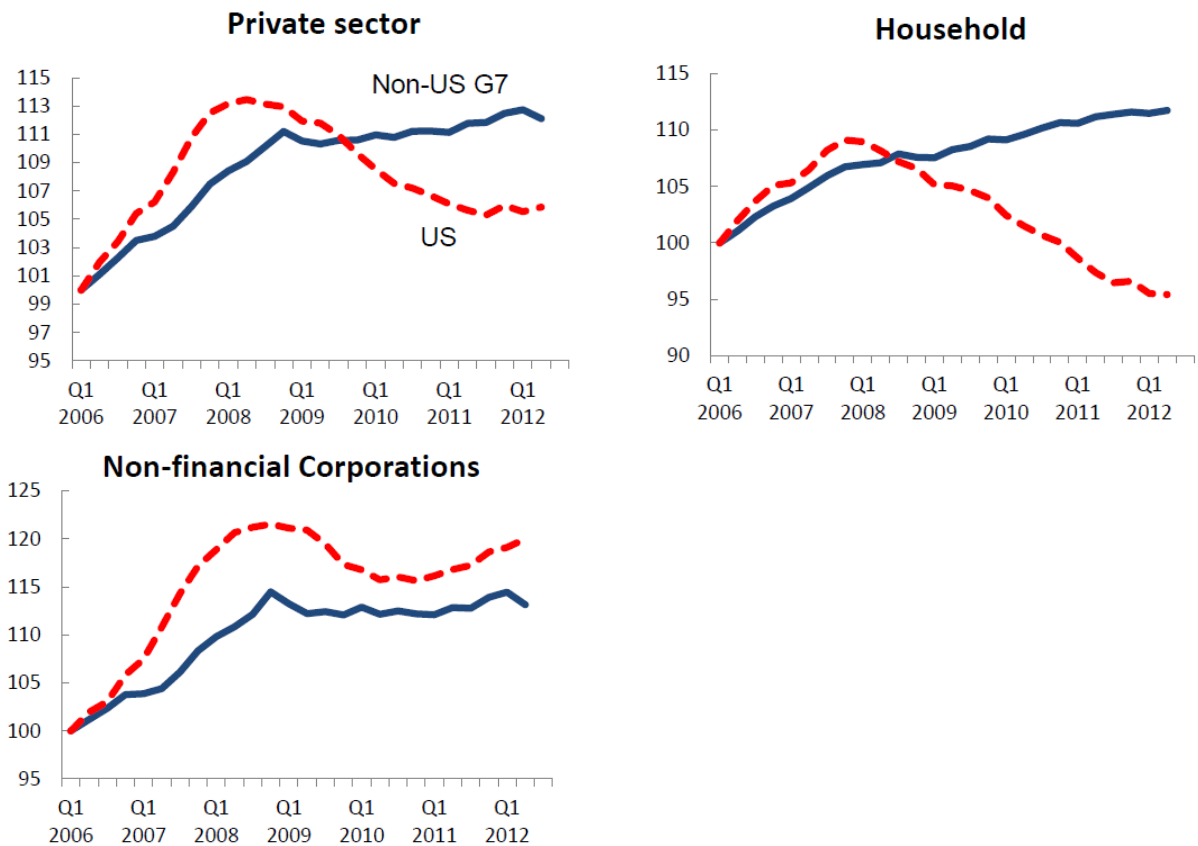
Source: Bank for International Settlements, Long series on credit to private non-financial sectors. The credit series are divided by the GDP deflator and normalized at 100 in 2006:Q1. The non-US G7 series is computed using relative PPP-adjusted GDP weights.

39

Figure 5. Symmetric Equilibria
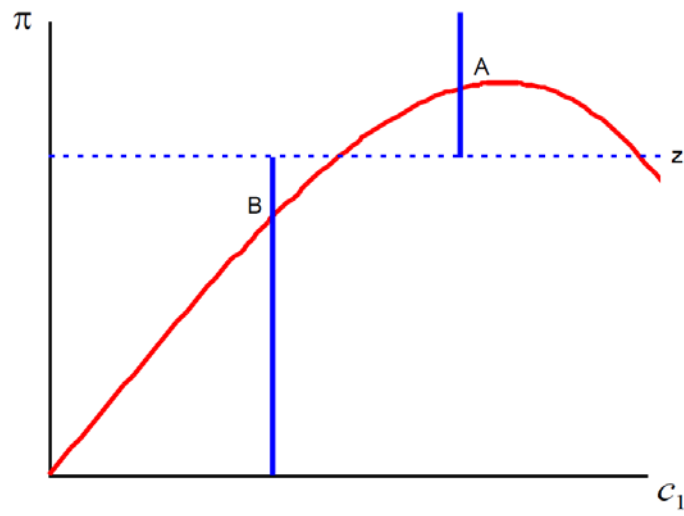
**Figure 6. All Equilibria: Role of Trade Integration**
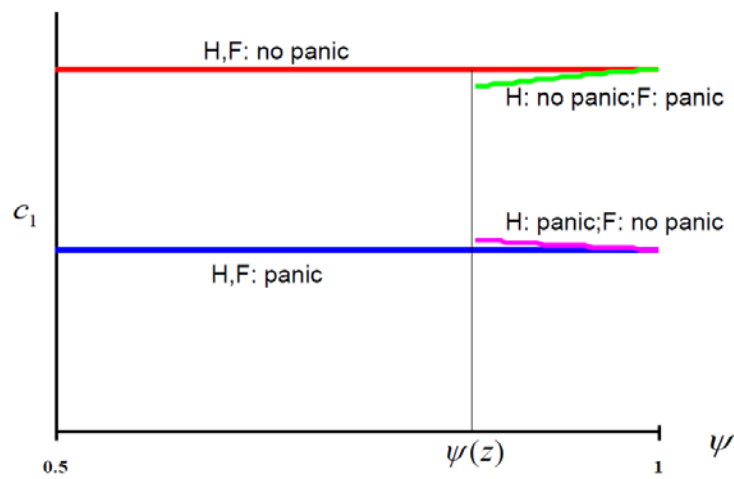
Figure 7. Corporate Profits
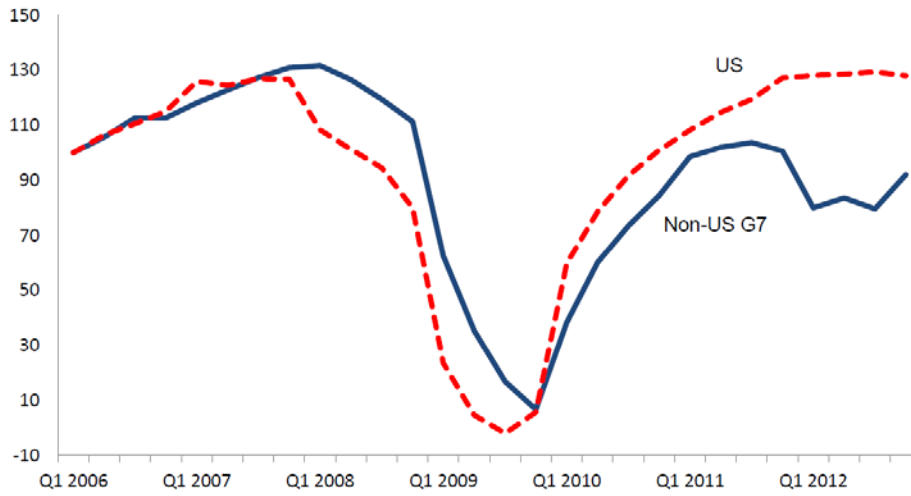
Source: Worldscope, Net profits (income). Profits are aggregated over continuing firms firms within each country, divided by the GDP deflator, and normalized at 100 in 2006:Q1. The non-US G7 series is computed using relative PPP-adjusted GDP weights.

Figure 8. On Existence of Asymmetric Equilibria*
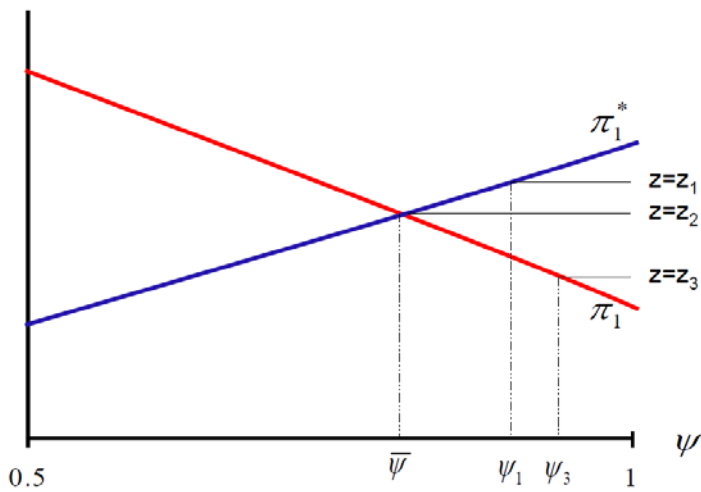
* The profit schedules are drawn under the assumption that there is a panic in Home and no panic in Foreign. When $z = z_i$ a mixed equilibrium exists as long as $\psi > \psi_1$ for i=1 and i=3. When $z = z_2$ a mixed equilibrium exists as long as $\psi > \overline{\psi}$.

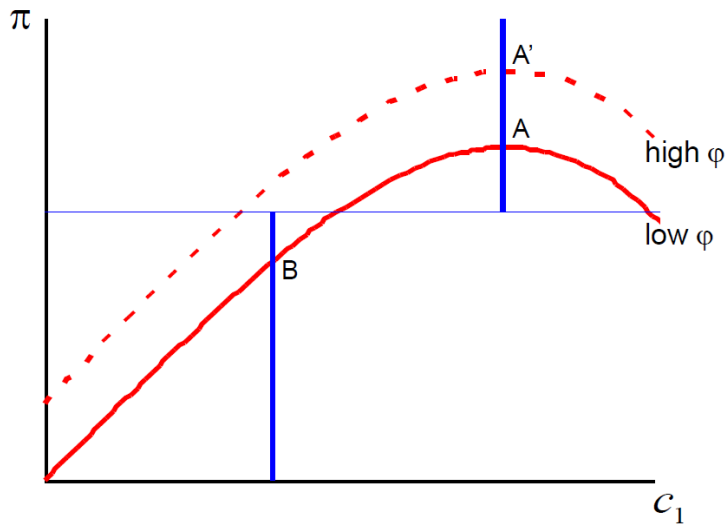**Figure 9. Panic Vulnerability: Role of Credit**

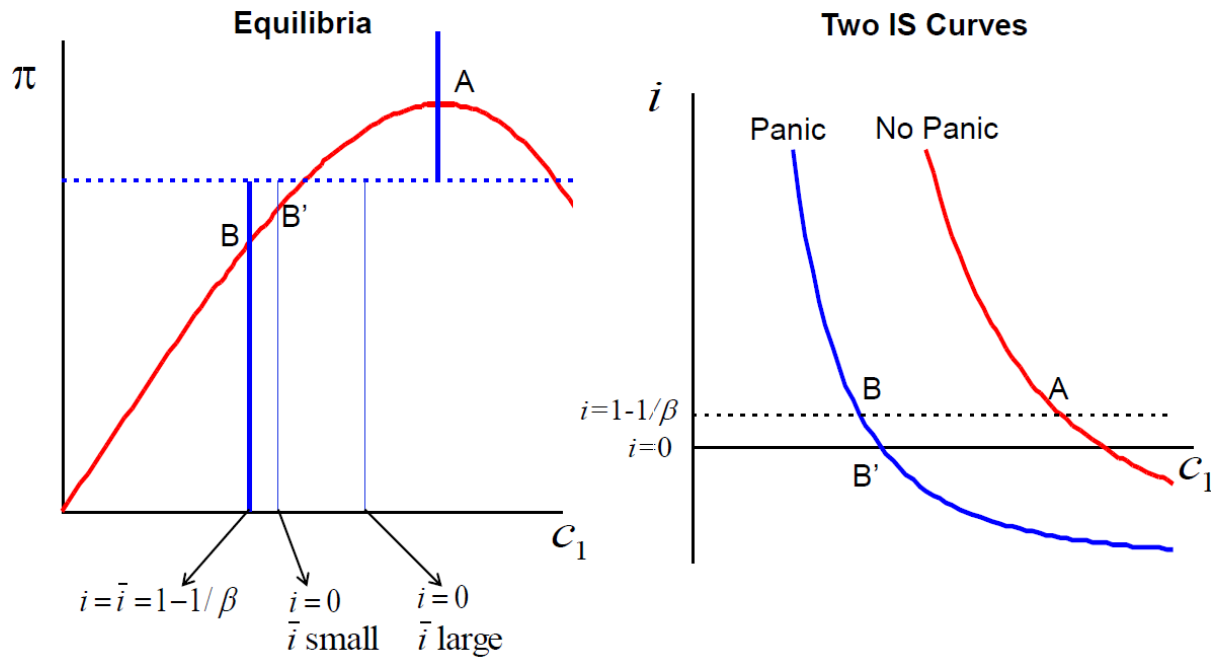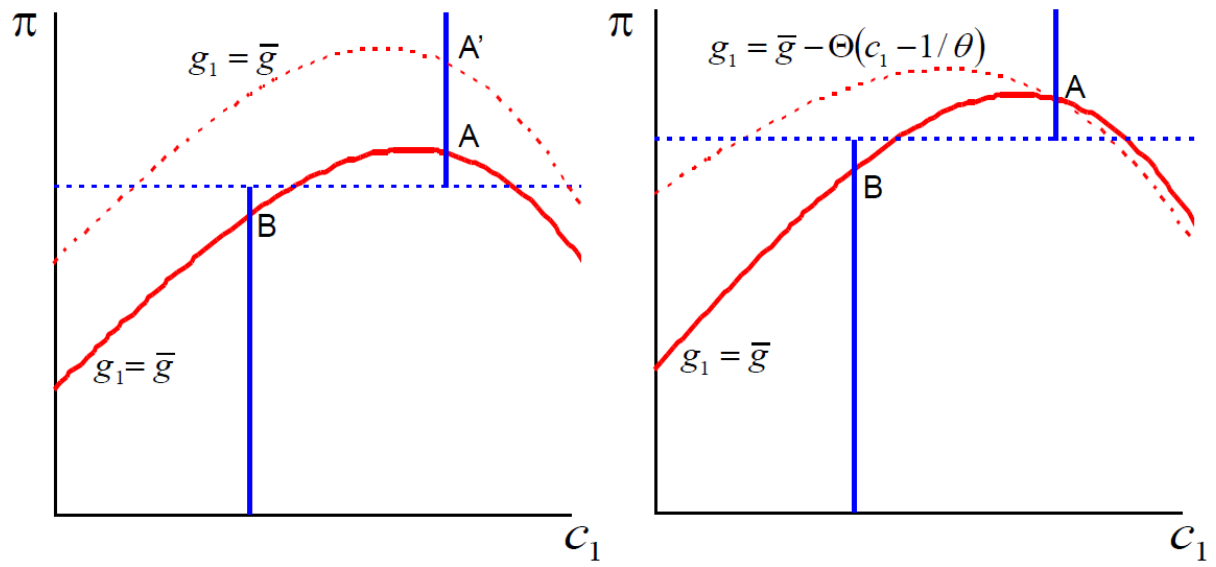**Figure 10. Panic Vulnerability: Role of Monetary Policy**

Figure 11. Panic Vulnerability: Role of Fiscal Policy*

Appendix

A. GDP Forecast Expectation and Variance

This Appendix describes in some more detail how the numbers in Figure 3 are computed. The data has been purchased from Consensus Economics. In their January newsletter of "Consensus Forecast" and "Asia Pacific Consensus Forecasts" they publish one-year-ahead GDP forecast probabilities since 1999 for the countries listed in the Figure. More specifically, for every country and year there are seven intervals of growth forecasts (e.g. 1-2%, 2-3%). The precise intervals may change from year to year. The data reports probabilities of each interval as the percentage of forecasts that lie in that interval. We compute the expectation and variance of the forecasts by using the midpoint of each interval, together with the probabilities of the intervals.

One issue is that the intervals at both ends of the range are not bounded (e.g., an interval can be " < - 1%"). In that case we adopt two scenarios to choose a midpoint for the interval. In the first scenario, we choose a midpoint by assuming that the interval width is the same as that for the other intervals. In the second scenario we choose a midpoint by assuming that the interval width is twice that for the other intervals. This leads to almost identical results. Figure 3 shows the results for the first scenario.

B. Model Equilibrium

In this Appendix we show how the model can be described a set of eight equations. Throughout the paper we use these equations to look at various special cases. These equations are:

$$\frac{\mu}{\mu-1}\frac{\lambda}{\alpha A}c_2^{\gamma}\frac{P_2}{P_{H,2}}\left(\frac{P_2}{P_{H,2}}c_2+g_2\right)^{\frac{1-\alpha}{\alpha}}=n^{\kappa} \tag{68}$$

$$\frac{\mu}{\mu-1}\frac{\lambda}{\alpha A}(c_2^*)^{\gamma}\frac{P_2^*}{P_{F,2}}\left(\frac{P_2^*}{P_{F,2}}c_2^*+g_2^*\right)^{\frac{1-\alpha}{\alpha}}=(n^*)^{\kappa} \tag{69}$$

$$c_1^{-\gamma}=\beta(1+i)c_2^{-\gamma} \tag{70}$$

$$[c_1^*]^{-\gamma}=\beta(1+i^*)[c_2^*]^{-\gamma} \tag{71}$$

$$\pi=c_1+\frac{P_{H,1}}{P_1}g_1-\frac{\lambda}{A}c_1^{\gamma}\left(\frac{P_1}{P_{H,1}}c_1+g_1\right)^{1/\alpha} \tag{72}$$

$$+\frac{\phi}{1+i}\frac{\kappa\lambda}{A}c_2^{\gamma}n^{-\frac{\mu}{(\mu-1)\alpha}}\left[\frac{P_2}{P_{H,2}}c_2+g_2\right]^{1/\alpha}$$

$$\pi^*=c_1^*+\frac{P_{F,1}}{P_1^*}g_1^*-\frac{\lambda}{A}(c_1^*)^{\gamma}\left(\frac{P_1^*}{P_{F,1}}c_1^*+g_1^*\right)^{1/\alpha} \tag{73}$$

$$+\frac{\phi}{1+i^*}\frac{\kappa\lambda}{A}(c_2^*)^{\gamma}(n^*)^{-\frac{\mu}{(\mu-1)\alpha}}\left[\frac{P_2^*}{P_{F,2}}c_2^*+g_2^*\right]^{1/\alpha}$$

$$n=\begin{matrix}\overline{n} & \text{if } \pi<z \\ 1 & \text{if } \pi\geq z\end{matrix} \tag{74}$$

$$n^*=\begin{matrix}\overline{n} & \text{if } \pi^*<z \\ 1 & \text{if } \pi^*\geq z\end{matrix} \tag{75}$$

With relative prices as in (36), these are 8 equations in c_1, c_1^*, c_2, c_2^*, n, n^*, π and π^*. They are derived as follows. (68) follows by substituting the labor supply schedule $W_2/P_2=\lambda c_2^{\gamma}$ and $P_{H,2}(j)/P_{H,2}=n^{1/(\mu-1)}$ into the optimal price setting equation (20). It also uses the expression (19) for $y_2(j)$ that enters into the optimal price setting equation (20), after substituting (35) into the expression for $y_2(j)$. (69) is the Foreign counterpart of (68). (70) follows from the intertemporal consumption Euler equation (8) after substituting the zero inflation monetary policy ($P_2=P_1$). (71) is the Foreign counterpart.

(72) is an expression for available funds $\pi=\pi_1+\phi\pi_2/(1+i)$. It is derived as follows. First, we derive π_1, which is on the first line of the right hand side of (72). It is equal to

$$\pi_1=\frac{P_{H,1}}{P_1}y_1(j)-\frac{W_1}{P_1}\frac{1}{A}y_1(j)^{1/\alpha} \tag{76}$$

Using that $P_{H,1}(j)=P_{H,1}$, we have from (29) that $y_1(j)=c_{H,1}+c_{H,1}^*+g_1$. Substituting $c_{H,1}=\psi(P_1/P_{H,1})c_1$ and $c_{H,1}^*=(1-\psi)(S_1P_1^*/P_{H,1})c_1^*$, and also using $P_1c_1=S_1P_1^*c_1^*$ from (35), we have $y_1(j)=(P_1/P_{H,1})c_1+g_1$. When we substitute this into (76), together with $W_1/P_1=\lambda c_1^{\gamma}$, we get the first line on the right hand side of (72). The second line is $\phi\pi_2/(1+i)$. We derive an expression

for π_2 as follows. From (21) it is equal to $\pi_2(j) = \kappa \dfrac{1}{A}(W_2/P_2)y_2(j)^{1/\alpha}$. We substitute $W_2/P_2 = \lambda c_2^\gamma$ and the expression (19) for $y_2(j)$. In the expression for $y_2(j)$ we also substitute (35) and $P_{H,2}(j)/P_{H,2} = n^{1/(\mu-1)}$. This then delivers the second line on the right hand side of (72). (73) is the Foreign counterpart. Finally, (74) follows from the bankruptcy condition (26) and (75) is its Foreign counterpart.

The paper considers two special cases of this system of equations. In sections 2.5 and 3.1-3.4 we assume $g_t = 0$ and in the vulnerability section 4 we assume $\zeta = \alpha = 1$. We will now show that $g_t = 0$ allows us to summarize the equilibrium in the form of the 6 equations (37)-(42) and that $\zeta = \alpha = 1$ implies the symmetric equilibrium given by (54)-(56) in the vulnerability section.

Setting $g_2 = g_2^* = 0$ and taking (68)-(69) to the power $\alpha/(1-\alpha+\alpha\gamma)$, these two equations can be written as

$$\theta\left(\frac{P_2}{P_{H,2}}\right)^{\frac{1}{1-\alpha+\alpha\gamma}} c_2 = n^\zeta \tag{77}$$

$$\theta\left(\frac{P_2^*}{P_{F,2}}\right)^{\frac{1}{1-\alpha+\alpha\gamma}} c_2^* = n^{*\zeta} \tag{78}$$

with θ and ζ defined in Section 2.5. Substituting the expressions for relative prices from (36), this gives two equations in c_2 and c_2^* that can be solved as a function of n and n^*. Using that $c_1 = [\beta(1+i)]^{-1/\gamma} c_2$ and $c_1^* = [\beta(1+i^*)]^{-1/\gamma} c_2^*$ from the consumption Euler equations (70)-(71), we then have

$$c_1 = \frac{[\beta(1+i)]^{-1/\gamma}}{\theta} n^{(1-\delta)\zeta}(n^*)^{\delta\zeta} \tag{79}$$

$$c_1^* = \frac{[\beta(1+i^*)]^{-1/\gamma}}{\theta} n^{\delta\zeta}(n^*)^{(1-\delta)\zeta} \tag{80}$$

This corresponds to the equilibrium equations (37)-(38) in Section 2.5 for the case where monetary policy is $(1+i)\beta = (1+i^*)\beta = 1$. (39)-(40) follow directly from (72)-(73) after again setting

$(1+i)\beta = (1+i^*)\beta = 1$ and $g_t = g_t^* = 0$. This monetary policy also implies $c_2 = c_1$ and $c_2^* = c_1^*$. We therefore replace second period with first-period consumption on the second lines of (72)-(73). We also use that the second period relative prices are equal to the first period relative prices. This follows from (36), together with $c_2 = c_1$ and $c_2^* = c_1^*$. Finally, (41)-(42) correspond exactly to (74)-(75).

In the vulnerability section 4 we only consider symmetric equilibria, under the assumption that $\alpha = \zeta = 1$. All relative prices are then equal to 1. It then follows immediately from (68) that $c_2 = n/\theta$. Together with the consumption Euler equation (70) this gives (54). (55) follows from (72) after substituting $c_2 = n/\theta$, setting $\alpha = \zeta = 1$ and setting all relative prices equal to 1.

Finally, a couple of brief comments are in order about the flexible price equilibrium for the case where $g_t = 0$, discussed at the end of Section 2.5. In that case there are two additional variables to solve for, the nominal interest rates i and i^*. There are also two additional equations, which are the period-1 analogues of (68)-(69), which follow from optimal price setting in period 1. Solving these equations for period 1, using the expression (36) for the relative price and the fact that the number of firms is 1 in period 1, gives $c_1 = c_1^* = 1/\theta$. This in turn implies that $\pi_1 = \pi_1^* = [\mu(1-\alpha)+\alpha]/(\mu\theta)$. Under Assumption 1, it follows that $\pi_1 > z$, so that also $\pi > z$ as $\pi_2 > 0$. Therefore no firms go bankrupt and $n = 1$. Similarly we also have $n^* = 1$. Solving for (68)-(69) with $g_2 = 0$ we then also have $c_2 = c_2^* = 1/\theta$. First and second period consumption are therefore equal and it follows from the consumption Euler equations (70)-(71) that $(1+i)\beta = (1+i^*)\beta = 1$.

C. Proof of Proposition 2

We already know that both symmetric equilibria exist when $\pi(\overline{n}) < z < \pi(1)$. We therefore focus on the existence of asymmetric equilibria. We will only consider the asymmetric equilibrium $(n,n^*) = (\overline{n},1)$ as the other asymmetric equilibrium, $(n,n^*) = (1,\overline{n})$, exists if and only if the first one exists.

From (37)-(38), setting $n = \overline{n}$ and $n^* = 1$ gives $c_1 = (1/\theta)\overline{n}^{(1-\delta)\zeta}$ and $c_1^* = (1/\theta)\overline{n}^{\delta\zeta}$. Substituting these values for c_1 and c_1^* into (39)-(40) gives

$$\hat{\pi}(\psi) = \frac{1}{\theta}\overline{n}^{(1-\delta)\zeta}\left(1 - \frac{(\mu-1)\alpha}{\mu}\overline{n}^{\kappa}\right) + \phi\beta\frac{\mu(1-\alpha)+\alpha}{\mu\theta}\overline{n}^{\zeta(1-\delta)-1}$$

$$\hat{\pi}^*(\psi) = (1+\phi\beta)\frac{\mu(1-\alpha)+\alpha}{\mu\theta}\bar{n}^{\zeta\delta}$$

where $\hat{\pi}(\psi)$ and $\hat{\pi}^*(\psi)$ are the values of π and π^* when $(n,n^*) = (\bar{n},1)$ and $\delta = (1-\psi)/[(1-\alpha+\alpha\gamma)(2\psi-1)+2(1-\psi)]$. We will consider values of ψ between 0.5 and 1. The asymmetric equilibrium $(n,n^*) = (\bar{n},1)$ exists when $\hat{\pi}(\psi) < z \le \hat{\pi}^*(\psi)$. This is clearly the case for $\psi = 1$ as $\hat{\pi}(1) = \pi(\bar{n})$ and $\hat{\pi}^*(1) = \pi(1)$.

Using the negative relationship between ψ and δ, it follows immediately from the expressions for $\hat{\pi}$ and $\hat{\pi}^*$ above that the derivative of $\hat{\pi}$ with respect to ψ is negative and the derivative of $\hat{\pi}^*$ with respect to ψ is positive for ψ between 0.5 and 1. We will also show that there is a value $\bar{\psi} > 0.5$ for which $\hat{\pi}(\bar{\psi}) = \hat{\pi}^*(\bar{\psi})$. These two results together imply the proposition. As we lower ψ below 1, $\hat{\pi}$ rises and $\hat{\pi}^*$ falls, until we reach a level $\psi(z) > 0.5$ so that either $\hat{\pi}(\psi(z)) = z$ or $\hat{\pi}^*(\psi(z)) = z$. If this were not the case, then $\hat{\pi}(\psi) < \hat{\pi}^*(\psi)$ for all ψ between 0.5 and 1, which is inconsistent with the finding that they are equal for $\psi = \bar{\psi} > 0.5$. For values of ψ above $\psi(z)$ we have $\hat{\pi} < z$ and $\hat{\pi}^* > z$, so that $(n,n^*) = (\bar{n},1)$ is an equilibrium. For values of ψ below $\psi(z)$ we either have $\hat{\pi} > z$ or $\hat{\pi}^* < z$, so that $(n,n^*) = (\bar{n},1)$ is not an equilibrium.

We finally need to show that there is a value $\bar{\psi} > 0.5$ for which $\hat{\pi}(\bar{\psi}) = \hat{\pi}^*(\bar{\psi})$. Let the corresponding value of δ be $\bar{\delta}$. Equating the expressions above for $\hat{\pi}$ and $\hat{\pi}^*$ gives

$$\bar{n}^{(1-2\bar{\delta})\zeta} = \frac{(\alpha+\mu(1-\alpha))(1+\phi\beta)}{\mu-(\mu-1)\alpha\bar{n}^{\kappa}+\dfrac{\phi\beta(\mu(1-\alpha)+\alpha)}{\bar{n}}} \tag{81}$$

It follows from $\bar{n} < 1$ that the term on the right hand side is less than 1. Therefore it must be the case that $\bar{\delta} < 0.5$, from which it follows that $\bar{\psi} > 0.5$. It follows that there is a value $\psi = \bar{\psi} > 0.5$ for which $\hat{\pi}(\psi) = \hat{\pi}^*(\psi)$, which completes the proof of Proposition 2.

D. Introducing Wage Rigidities

In order to introduce wage rigidities we first introduce labor heterogeneity. Labor L_t in the production function is now a CES index of labor supply by all households:

$$L_t = \left(\int_0^1 L_t(j)^{\frac{\omega-1}{\omega}} dj \right)^{\frac{\omega}{\omega-1}} \tag{82}$$

where $L_t(j)$ is labor by agent j. Given L_t, this specification leads to the following demand for individual labor:

$$L_t(j) = \left(\frac{W_t(j)}{W_t} \right)^{-\omega} L_t \tag{83}$$

where $W_t(j)$ is the wage rate for labor supplied by agent j and

$$W_t = \left(\int_0^1 W_t(j)^{1-\omega} dj \right)^{\frac{1}{1-\omega}} \tag{84}$$

Aggregate labor demand in period t in the Home country is $n_{H,t}L_t$. Demand for labor supplied by agent j is then

$$1 - l_t(j) = \left(\frac{W_t(j)}{W_t} \right)^{-\omega} n_{H,t}L_t \tag{85}$$

We can now maximize agent j utility with respect to $W_t(j)$. All households choose the same optimal $W_t(j)$, which will then be equal to W_t. We will replace the λl_t in the utility function with $\tilde{\lambda} l_t$. Dropping the j, maximization of utility with respect to the individual wage rate gives

$$\frac{W_t}{P_t} = \lambda c_t^\gamma \tag{86}$$

where $\lambda = \tilde{\lambda}\omega/(\omega-1)$. With the redefined λ this is the same as (13). Nothing else in the model changes.

When wages are rigid, they are set at the start of each period. This makes no difference for period 2 as there are no shocks during period 2. For period 1 the only shock is a self-fulfilling panic. We assume that the probability of a panic is infinitesimal. Then the right hand side of (86) needs to include the expectation of c_1^γ at the start of period 1 giving infinitesimal weight to a panic occurrence. The expectation is therefore based on $c_1 = 1/\theta$, its value in the absence of a panic. When the real wage

is set at the start of period t, it will then be set at λ/θ^γ. If instead the nominal wage is set, it will be equal to $\overline{P}\lambda/\theta^\gamma$, where $\overline{P}$ is the price index in the non-panic state. This is equal to P_{H1}, the price set at the start of period 1 by all firms. The real wage will then be $(P_{H,1}/P_1)(\lambda/\theta^\gamma)$, where $P_{H,1}/P_1$ depends on c_1^*/c_1 as in (36).